1	Supporting Information for
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3	Fast Response of the Tropics to an Abrupt Loss of Arctic Sea Ice via Ocean Dynamics
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5	Kun Wang ^{1,2,3} , Clara Deser* ¹ , Lantao Sun ⁴ and Robert A. Tomas ¹
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7	1 National Center for Atmospheric Research, P.O. Box 3000, Boulder, CO 80307 USA
8	2 Laboratory for Climate and Ocean-Atmosphere Studies, Department of Atmospheric and
9	Oceanic Sciences, School of Physics, Peking University, Beijing, China
10	3 Department of Aviation Meteorology, College of Air Traffic Management, Civil Aviation
11	University of China, Tianjin, China
12	4 Cooperative Institute for Research in Environmental Sciences, University of Colorado Boulder
13	and NOAA Earth System Research Laboratory, Boulder CO 80305, USA
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16	Jan 27, 2018
17	Submitted to GRL
18	Revised March 31, 2018
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20	*Corresponding author address: Dr. Clara Deser, Climate and Global Dynamics Division,
21	National Center for Atmospheric Research, P.O. Box 3000, Boulder, CO 80307 USA. Email:
22	cdeser@ucar.edu Tel: 303-497-1359; Fax: 303-497-1333.

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27 Text S1

We compute the heat budget for the upper 100m of the eastern equatorial Pacific region (10°S10°N, 90°W-150°W) using the following equation:

$$30 \quad \rho_o C_p \int_{-H}^0 \frac{\partial T}{\partial t} dz = -\rho_o C_p \int_{-H}^0 \nabla \cdot (\boldsymbol{U}T) dz - \rho_o C_p \int_{-H}^0 \nabla \cdot \boldsymbol{K} dz + Q_{net} \quad (1)$$

where ρ_o is the reference density of seawater, C_p the specific heat of seawater, T is temperature, H=100m, *U* is the three-dimensional velocity, *K* is the diffusive temperature flux resulting from diapycnal diffusion and parameterized isopycnal diffusion, and Q_{net} is the net air-sea heat flux. The anomalous temperature tendency (TEND in Fig. 4a) is given by the sum of the advection term (first term on right hand side; ADV in Fig. 4a), the diffusion term (second term on right hand side; DIFF in Figs. 4a and 4b) and Q_{net} . The advection term can be divided into horizontal (ADV_h) and vertical (ADV_w) components as follows:

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$$ADVh = -\rho_o C_p \int_{-H}^0 \left(u' \frac{\partial \overline{T}}{\partial x} + \overline{u} \frac{\partial T'}{\partial x} + u' \frac{\partial T'}{\partial x} + v' \frac{\partial \overline{T}}{\partial y} + \overline{v} \frac{\partial T'}{\partial y} + v' \frac{\partial T'}{\partial y} \right) dz$$
(2)

39
$$ADVw = -\rho_o C_p \int_{-H}^0 \left(w' \frac{\partial \overline{T}}{\partial z} + \overline{w} \frac{\partial T'}{\partial z} + w' \frac{\partial T'}{\partial z} \right) dz$$
 (3)

40 where primed variables are anomalies and overbar variables are the climatology.

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In Fig. 4c, the first, second and third terms on the right-hand side of Eqn. (3) are denoted W'T̄,
W̄T', and W'T' for short, respectively.

44 With equation (2) and (3), equation (1) can be changed into

45 TEND-DIFF-Qnet =
$$ADVh+ADVw$$
 (4)

46 Note that the right-hand side of Eqn. (4) includes the decomposition terms

47
$$(u'\frac{\partial\overline{T}}{\partial x} + \overline{u}\frac{\partial T'}{\partial x} + u'\frac{\partial T'}{\partial x} + v'\frac{\partial\overline{T}}{\partial y} + \overline{v}\frac{\partial T'}{\partial y} + v'\frac{\partial T'}{\partial y} + w'\frac{\partial\overline{T}}{\partial z} + w'\frac{\partial T'}{\partial z} + w'\frac{\partial T'}{\partial z}).$$





Figure S1. Meridional streamfunction response (color shading; 10⁻⁹ kg s⁻¹) to an abrupt loss of 51 Arctic sea ice in FOM and SOM averaged over years (a, b) 6-25, (c, d) 41-60 and (e, f) 81-100. 52 Contours show the late 20^{th} century climatology (contour interval = $2 \times 10^{-9} \text{ kg s}^{-1}$; zero contour is 53 thickened). 54



Figure S2. Pressure vertical velocity (omega; Pa s¹) response across the Pacific averaged over 5°N-5°S (color shading) to an abrupt loss of Arctic sea ice in FOM and SOM averaged over years (a, b) 6-25, (c, d) 41-60 and (e, f) 81-100. Contours show the late 20th century climatology (contour interval = 0.01 Pa s⁴; negative values dashed). Positive (negative) values indicate downward (upward) motion.



Figure S3. Evolution of Pacific zonal-mean (a, b) SST (°C) and surface wind (m s⁻¹) and (c, d)
precipitation (mm d⁻¹) responses to an abrupt loss of Arctic sea ice in FOM and SOM. (e)
Climatological Pacific zonal-mean precipitation (mm d⁻¹). Note the different wind vector scales in
(a) and (b). The tropical (30N-30S) Pacific mean SST response at each time step has been removed
for clarity in (a) and (b).



Figure S4. SST (°C) and surface wind (m s⁻¹) responses to an abrupt loss of Arctic sea ice in FOM
 averaged over years (a) 6-25, (b) 41-60 and (c) 81-100.





Figure S5. Heat budget decomposition for temperature averaged over the layer 200-400m (T; °C) 79 80 in the region [10°S-10°N, 150°W-90°W] from FOM. The terms are defined as follows in units of °C s⁻¹: (a) ADV = total advection, DIFF = diffusion; (b) ADVw = vertical advection, ADVu = 81 82 zonal advection, ADVv = meridional advection; (c) VprTbr = meridional advection due to the anomalous meridional current acting on the mean meridional temperature gradient, VbrTpr = 83 meridional advection due to the mean meridional current acting on the anomalous meridional 84 temperature gradient, VprTpr = meridional advection due to the anomalous meridional current 85 acting on the anomalous meridional temperature gradient; (d) WprTbr = vertical advection due to 86 the anomalous vertical motion acting on the mean vertical temperature gradient, WbrTpr = vertical 87 advection due to the mean vertical motion acting on the anomalous vertical temperature gradient, 88 89 WprTpr = vertical advection due to the anomalous vertical motion acting on the anomalous vertical temperature gradient. 90 91



Figure S6. Depth-latitude sections of the temperature response (color shading; °C) superimposed
upon climatological mean isopycnals (contours; kg m⁻³) averaged over the longitude band (150°W90°W) to an abrupt loss of Arctic sea ice in FOM, averaged over years: (a) 6-25, (b) 21-40, (c) 4160, (d) 61-80 and (e) 81-100.



Figure S7. Heat budget decomposition for temperature averaged over the layer 200-400m (T; °C) in the region [30°S-10°S, 150°W-90°W] in FOM. The terms are defined as follows, in units of °C s^{-1} : (a) ADV = total advection, DIFF = diffusion; (b) ADVw = vertical advection, ADVu = zonal advection, ADVv = meridional advection; (c) WprTbr = vertical advection due to the anomalous vertical motion acting on the mean vertical temperature gradient, WbrTpr = vertical advection due to the mean vertical motion acting on the anomalous vertical temperature gradient, WprTpr = vertical advection due to the anomalous vertical motion acting on the anomalous vertical temperature gradient, We = Ekman pumping computed from the wind stress curl (10° cm s⁻¹).



Figure S8. Evolution of the AMOC response (Sv) to an abrupt loss of Arctic sea ice in FOM. AMOC is defined as the maximum meridional overturning streamfunction in the Atlantic sector.





Figure S9. Demonstration that the heat budget decomposition for temperature averaged over the 124 upper 100m in the region [10°S-10°S, 150°W-90°W] closes. Red curve shows the sum of the terms 125 on the left-hand side of Eqn. (4) in Text S1 (TEND – DIFF - Qnet); blue curve shows the sum of 126 the terms on the right-hand side of Eqn. (4) in Text S1 (ADVh + ADVw). The close match between 127 the red and blue curves indicates that our heat budget decomposition closes to a high degree of 128 129 accuracy.