

1 **High Predictability of Tropical Pacific Decadal Variability Dominated by**
2 **Oceanic Rossby Waves**
3 **(Supplementary material)**

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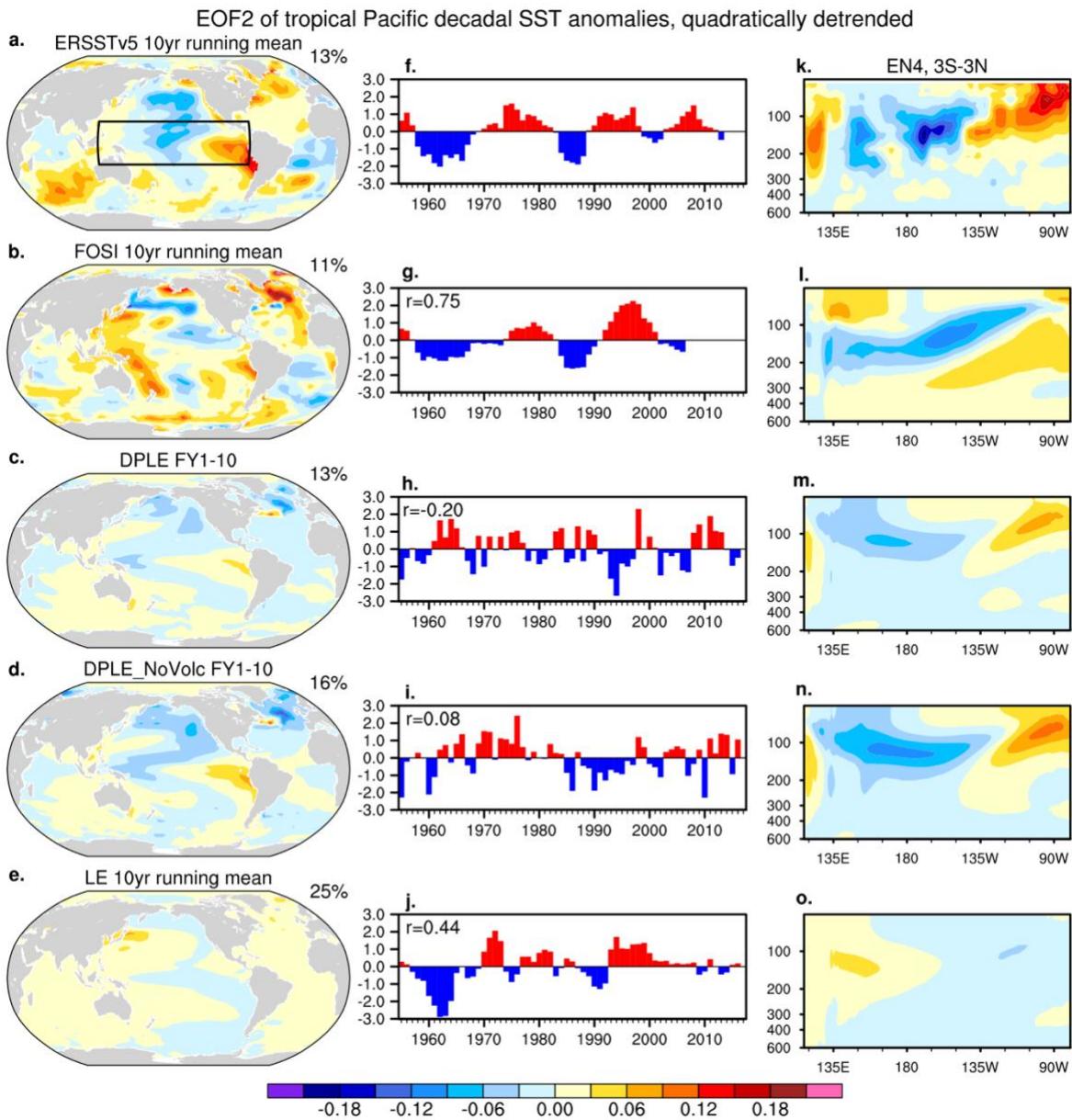
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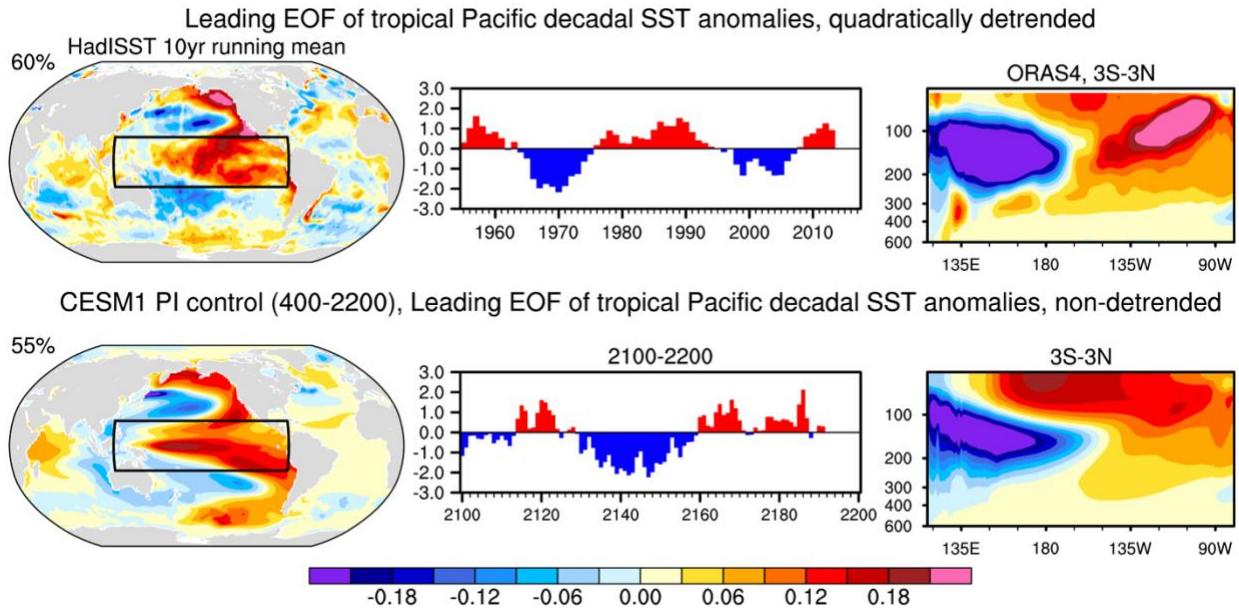
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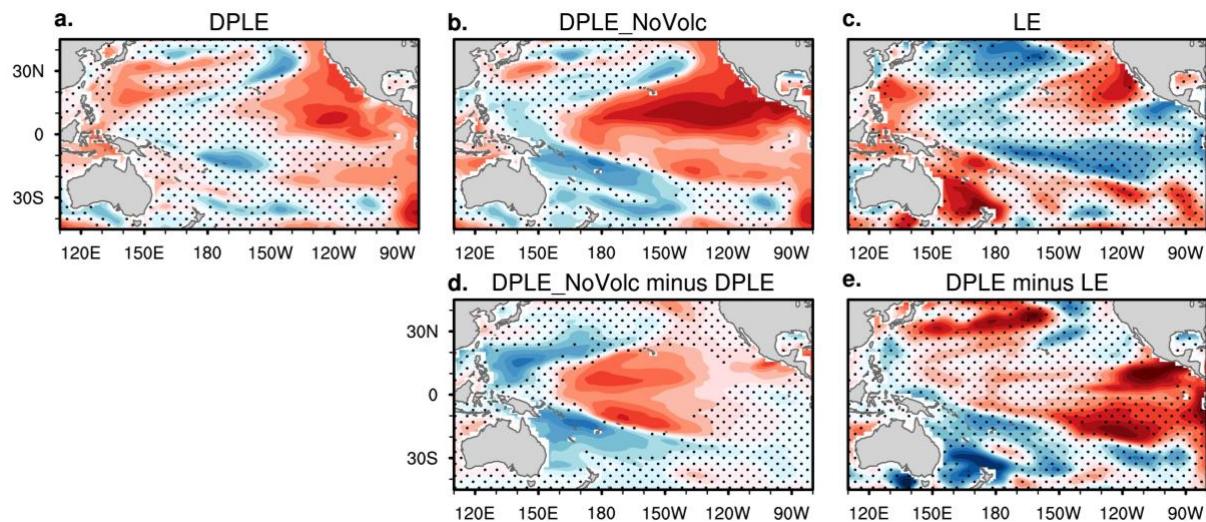
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Fig. S1 As in Fig. 1 but for the second leading EOF mode and PC2.

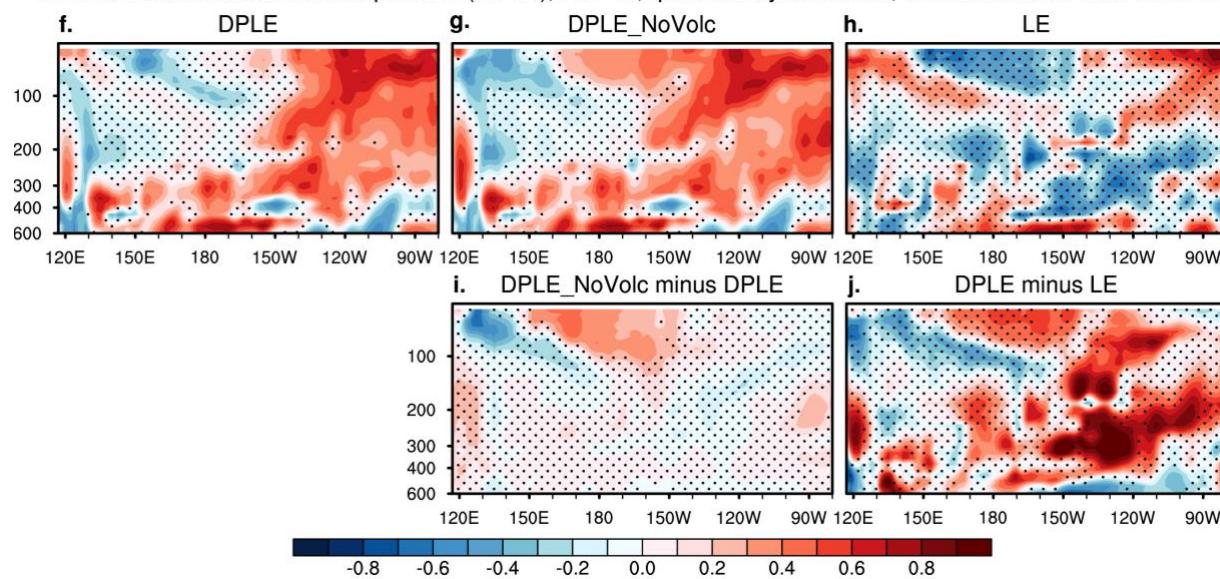


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 30 **Fig. S2 TPDV simulation in the alternative observational datasets and the CESM1 free-**
 31 **running preindustrial simulation.** As in Fig. 1 in the main text, but for (top row) HadISST
 32 (1955–2022) and ORAS4 (1958–2019), and (bottom) 1801-yr control simulation of CESM1 under
 33 the preindustrial forcing condition. The timeseries of standardized PC1 are only shown for the last
 34 101 years (2100–2200). The year in the axis indicates the start year of any 10-year average window.
 35 The numbers in the top-left corner of panels in the first column denote the percentage of total
 36 variance explained by the leading EOF mode in each dataset.

ACC of annual mean SST, FY1-10, quadratically detrended, verification data: ERSSTv5 1955-2022

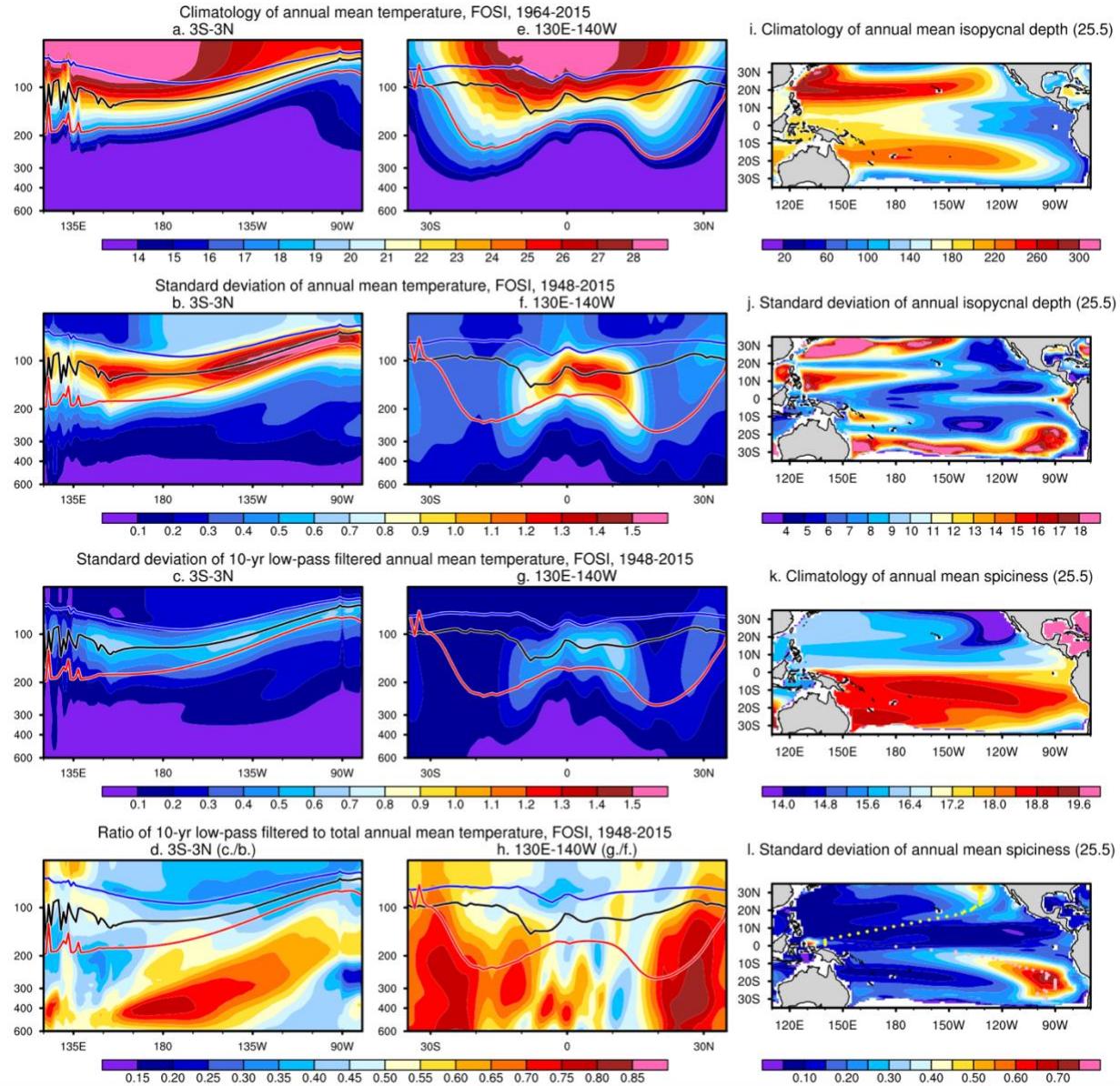


ACC of annual mean ocean temperature (3S-3N), FY1-10, quadratically detrended, verification data: EN4 1955-2022



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Fig. S3 As in Fig. 2 in the main text, but for skill evaluation relative to observations (SST in ERSSTv5, and ocean temperature in EN4).



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Fig. S4 Definition of different metrics capturing subsurface ocean temperature variability in FOSI. (a) Climatology and (b) standard deviation of equatorial Pacific (3°S – 3°N) subsurface ocean temperature, (c) standard deviation of 10-yr low-pass filtered component, and (d) standard deviation ratio of low-pass filtered component of total (non-detrended) annual mean temperature. (e-h) as in a-d but for the zonally averaged (130°E – 140°W) subsurface ocean temperature. The curves in a-h denote the climatological mixed layer depth (blue curves), thermocline depth (defined as the depth of maximum vertical temperature gradient; black curves), and isopycnal depth where the potential density is equal to 25.5 kg m^{-3} ($\sigma_{\theta}=25.5 \text{ kg m}^{-3}$; red curves). (i) Climatology and (j) standard deviation of annual mean isopycnal depth ($\sigma_{\theta}=25.5 \text{ kg m}^{-3}$). (k) Climatology and (l) standard deviation of annual mean spiciness [$^{\circ}\text{C}$; defined as temperature on the isopycnal depth ($\sigma_{\theta}=25.5 \text{ kg m}^{-3}$)]. The yellow and pink dots in l denote pathways where spiciness standard deviations are largest at each latitude.

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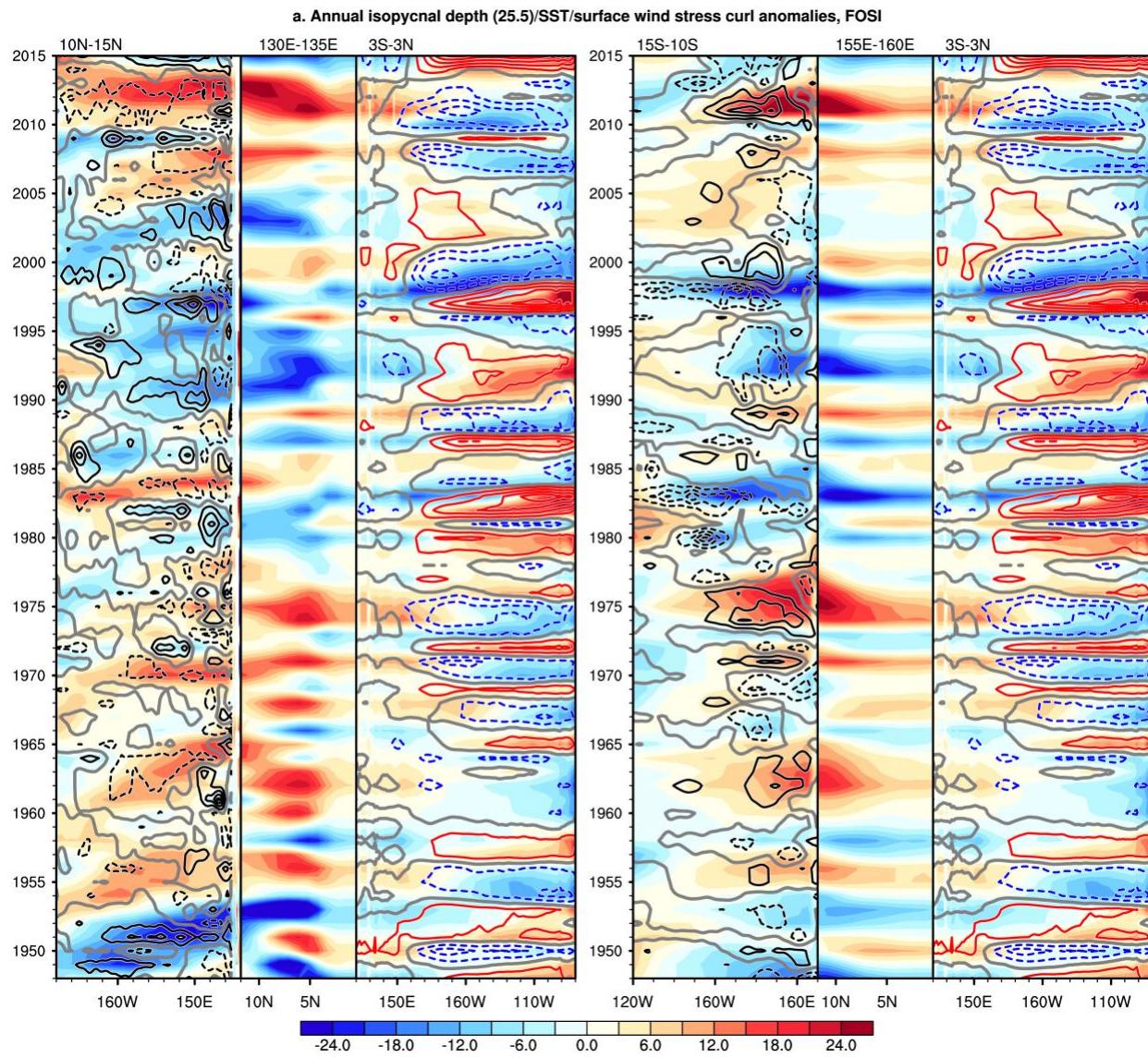
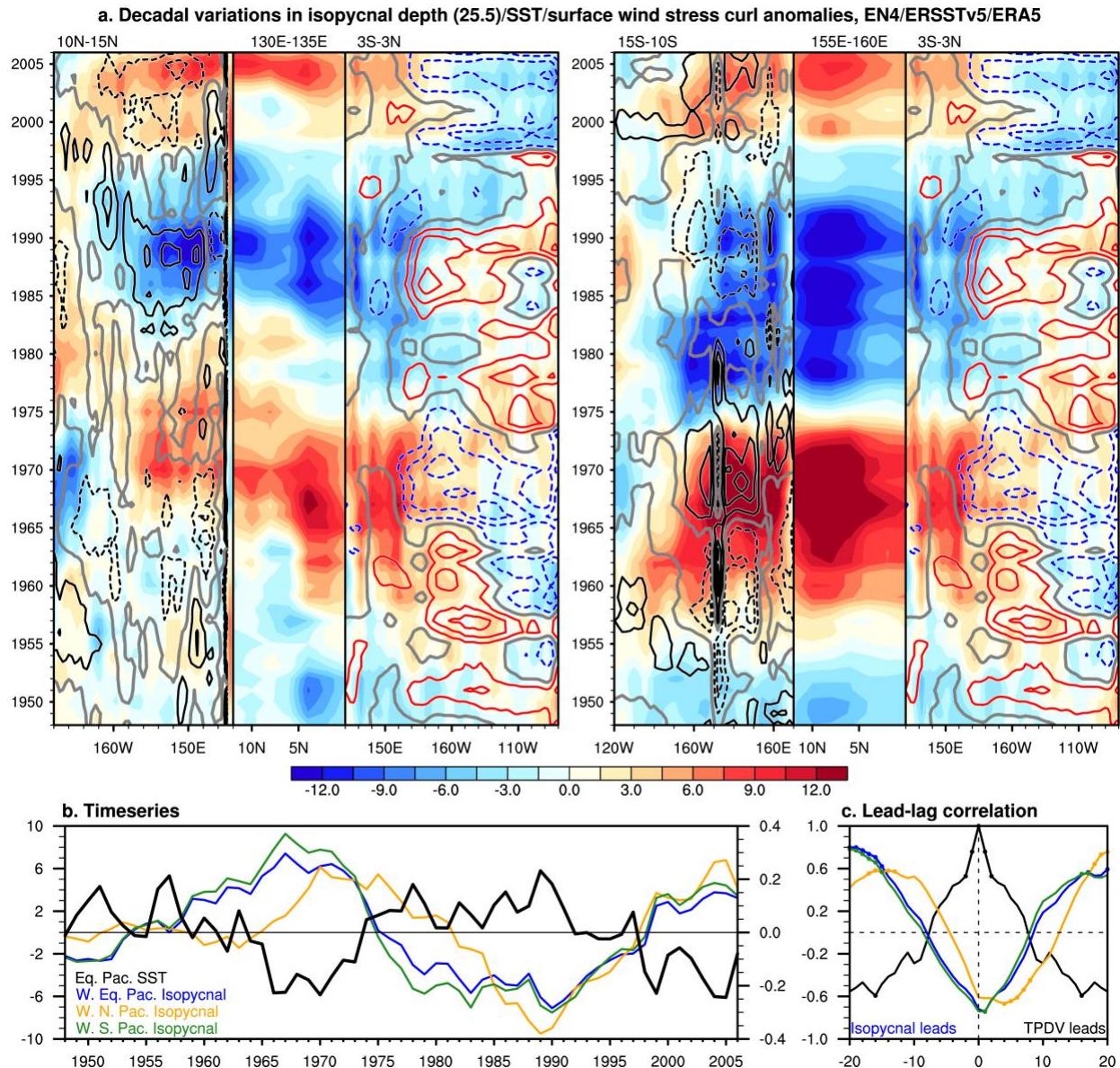
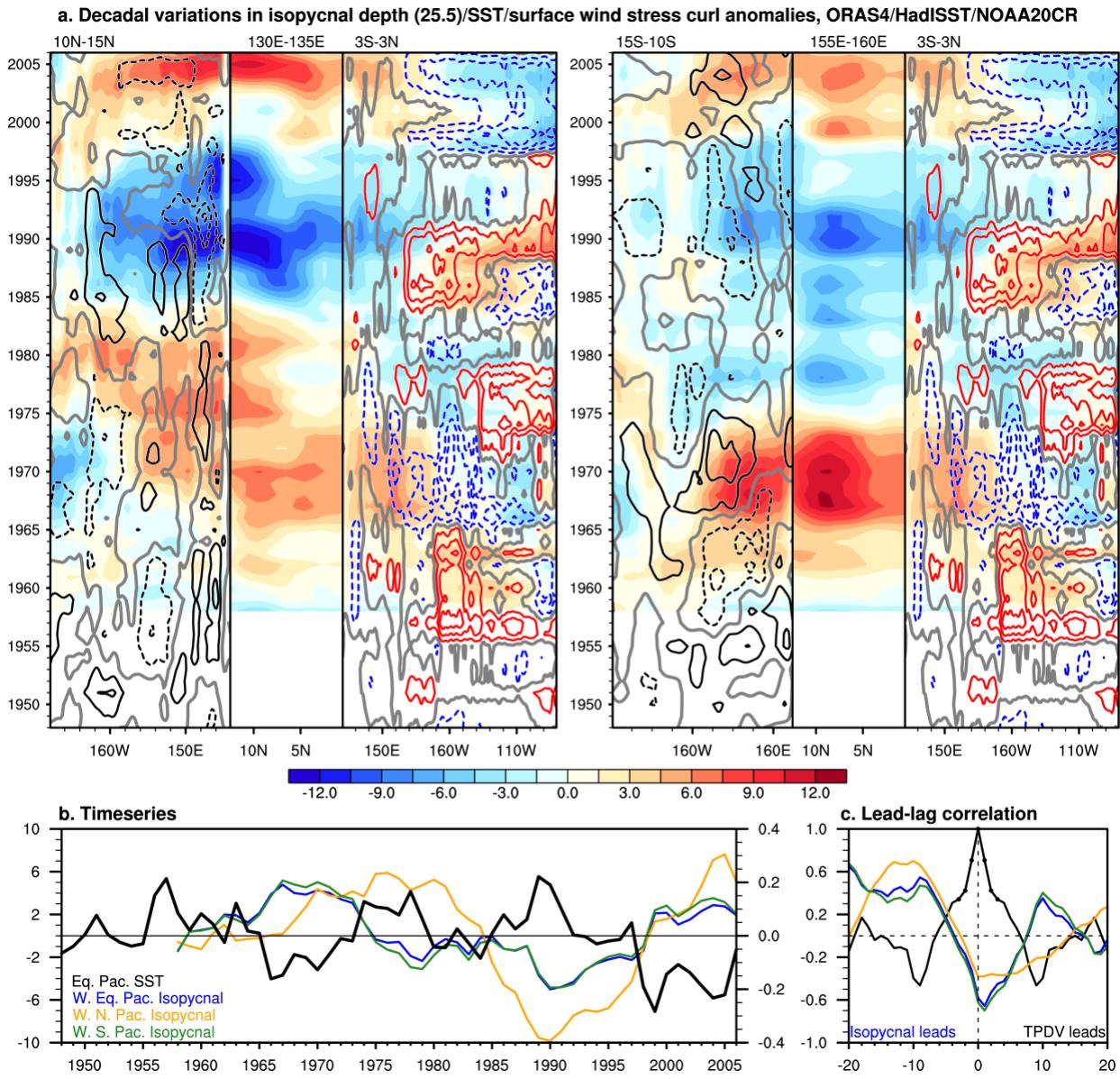


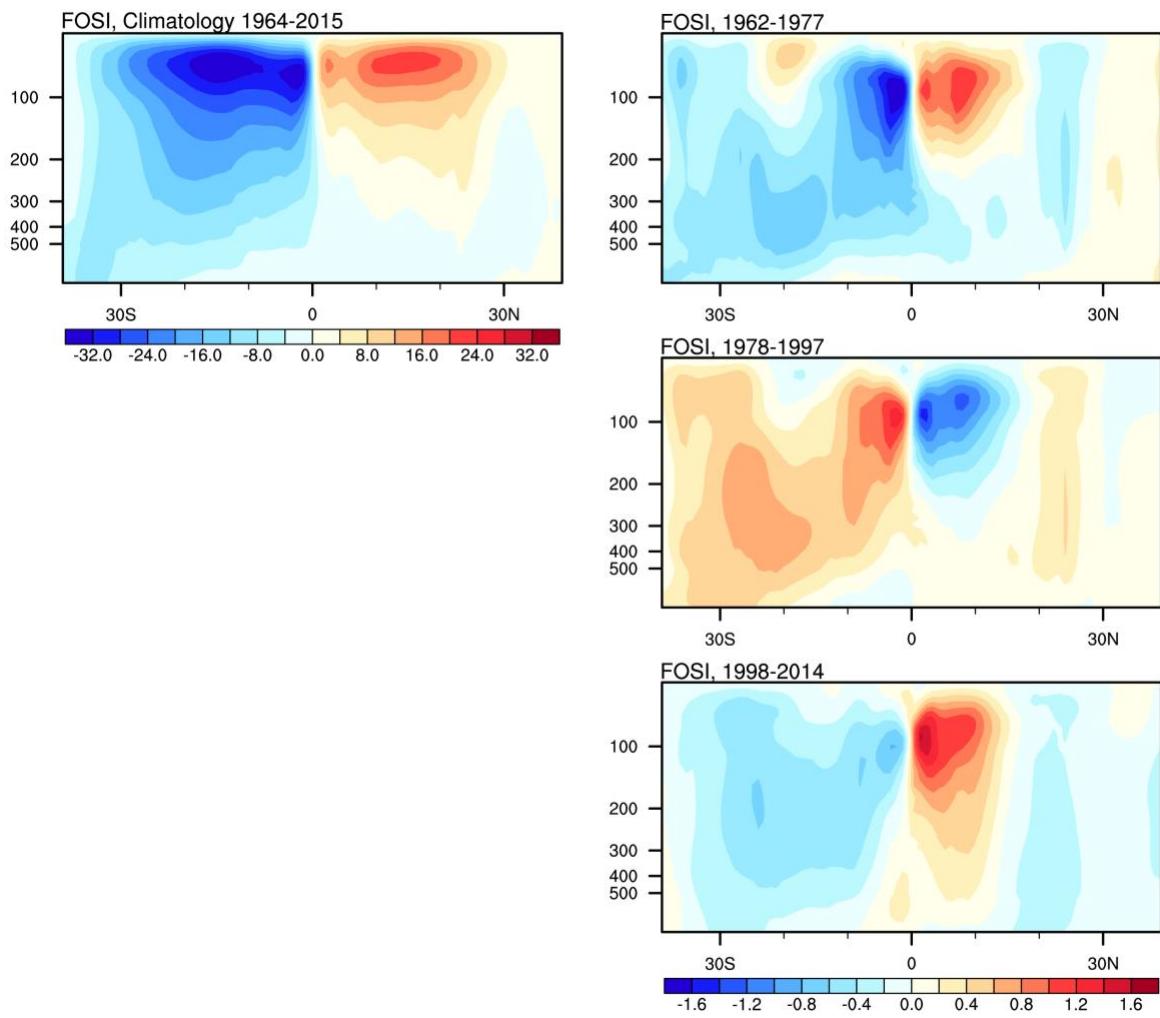
Fig. S5 As in Fig. 3a, but for non-filtered annual mean fields.





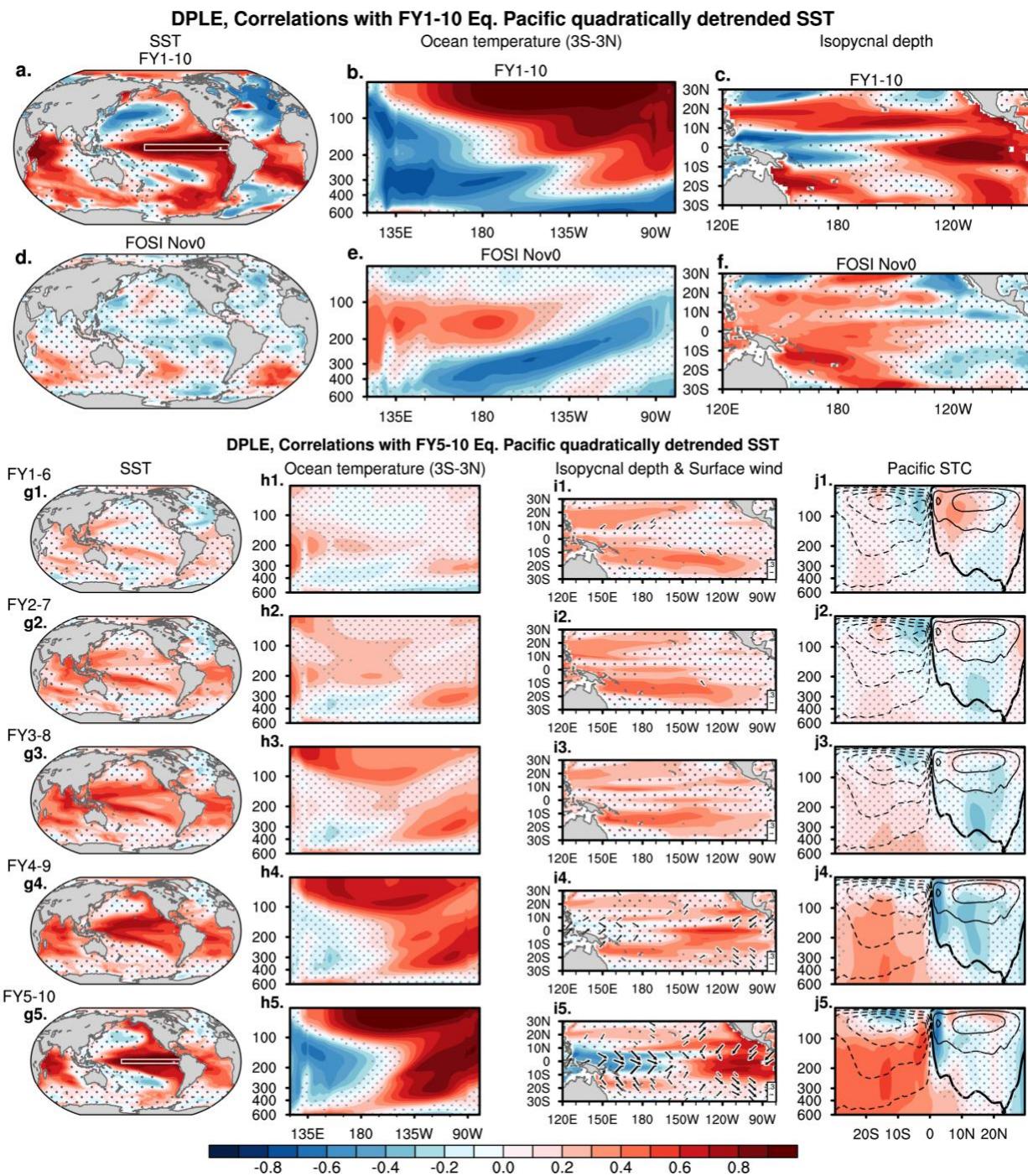
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Fig. S7 As in Fig. 3, but using ORAS4 for isopycnal depth, HadISST for SST, and NOAA 20CR for surface wind stress curl.



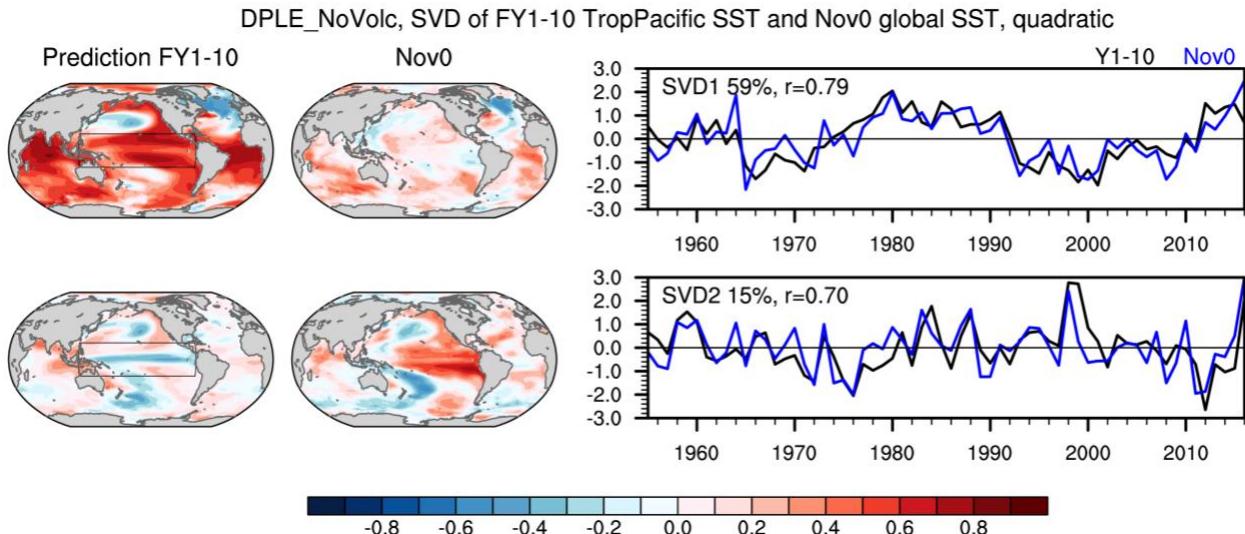
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62 **Fig. S8 STC climatology and anomalies associated with TPDV.** (top left) Climatology of ocean
63 overturning streamfunction (Sv) zonally averaged across the Pacific Ocean as a function of depth
64 (m) and latitude. Positive (negative) values of overturning streamfunction indicate clockwise (anti-
65 clockwise) orbit direction of the transport. (right) Anomalies during the negative TPDV phases
66 (1962–1977; 1998–2014) and positive TPDV phase (1978–1997).

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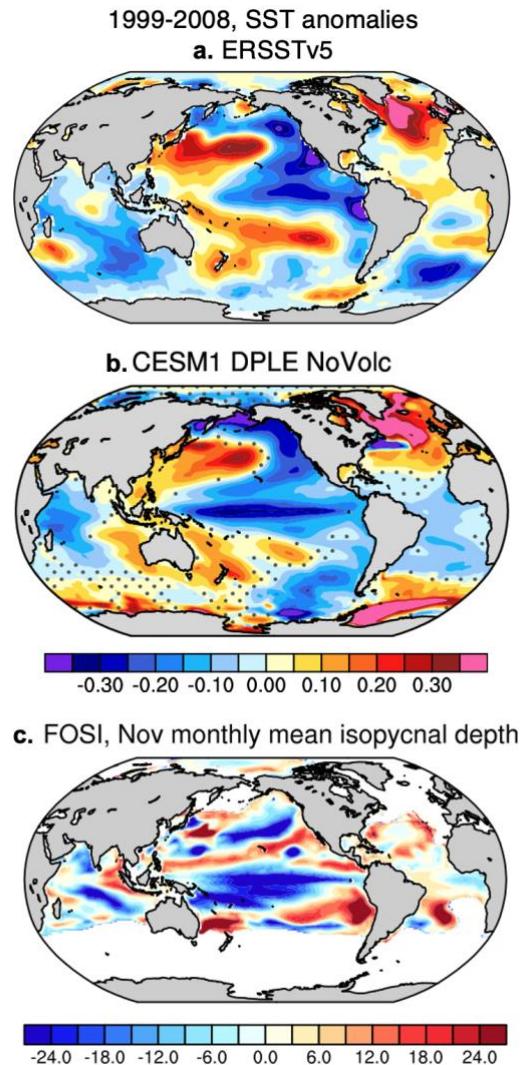


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69 **Fig. S9** As in Fig. 5, but for DPLE.



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 71 **Fig. S10** Pattern and timeseries associated with the (top row) first and (bottom row) second SVD
 72 modes of the covariance of predicted tropical Pacific (20°S – 20°N , 120°E – 120°W) SST anomalies
 73 in FY1–10 during 1955–2016, and global initial SST anomalies in Nov0 during 1954–2015. SVD1
 74 explains 59% of the total squared covariance, while SVD2 explains 15%. The expansion
 75 coefficients are correlated at a coefficient of 0.79 and 0.70 for SVD1 and SVD2, respectively. (left
 76 column) Regression maps of predicted SST at FY1–10 on the standardized Nov0 SST expansion
 77 coefficient (blue curve). (middle column) Regression maps of initial SST at Nov0 on the
 78 standardized FY1–10 SST expansion coefficient. (right column) Standardized time series of FY1–
 79 10 SST (black) and Nov0 SST (blue) expansion coefficients.
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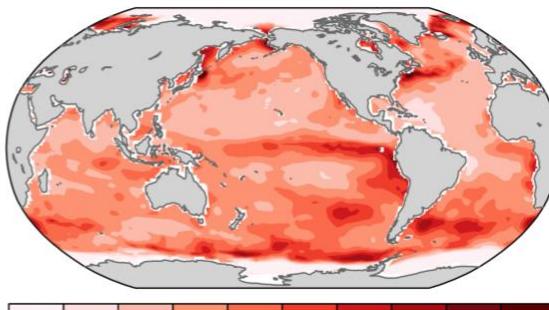
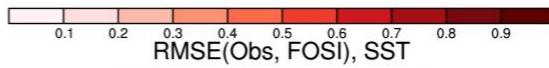
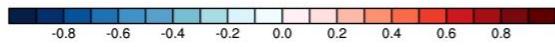
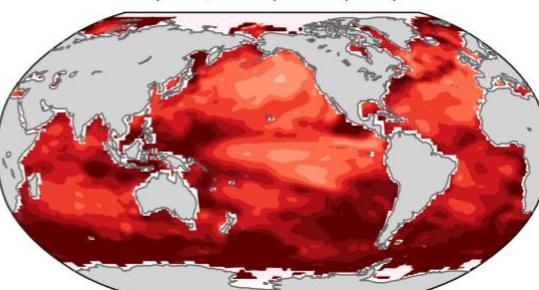


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Fig. S11 Quadratically detrended SST anomalies during 1999–2008 in (a) ERSSTv5 and (b) the 10-member ensemble-mean forecast initialized in November 1998 in DPLE_NoVolc using traditional drift correction method (see Methods). (c) Isopycnal depth anomalies (m; $\sigma_{\theta} = 25.5 \text{ kg m}^{-3}$) on November 1, 1998, in FOSI.

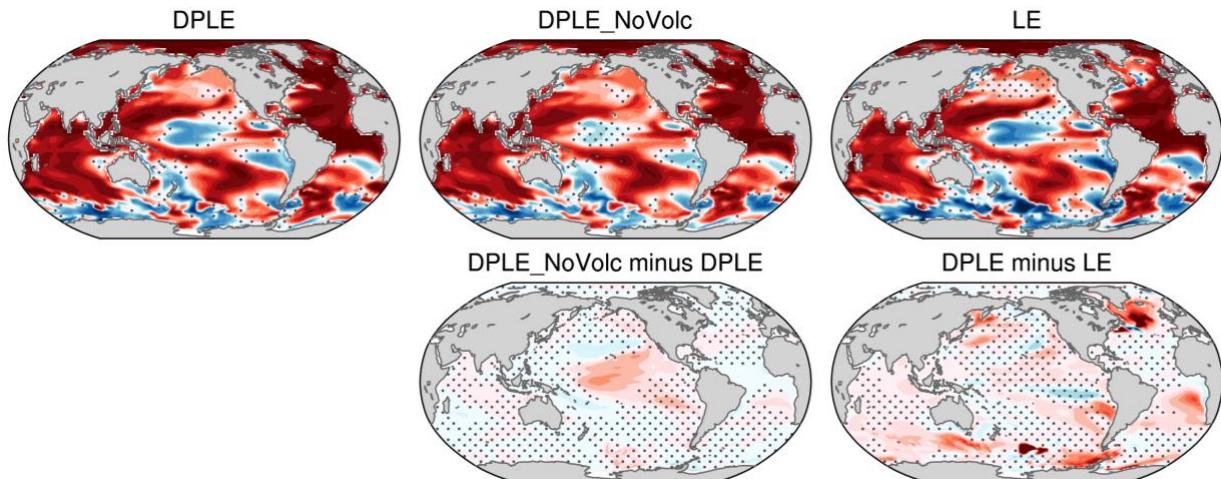
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Evaluation of FOSI initial condition anomalies in November, 1954-2015, nondetrend
Corr(Obs, FOSI), SST

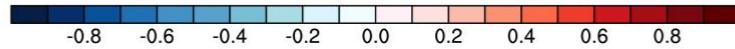
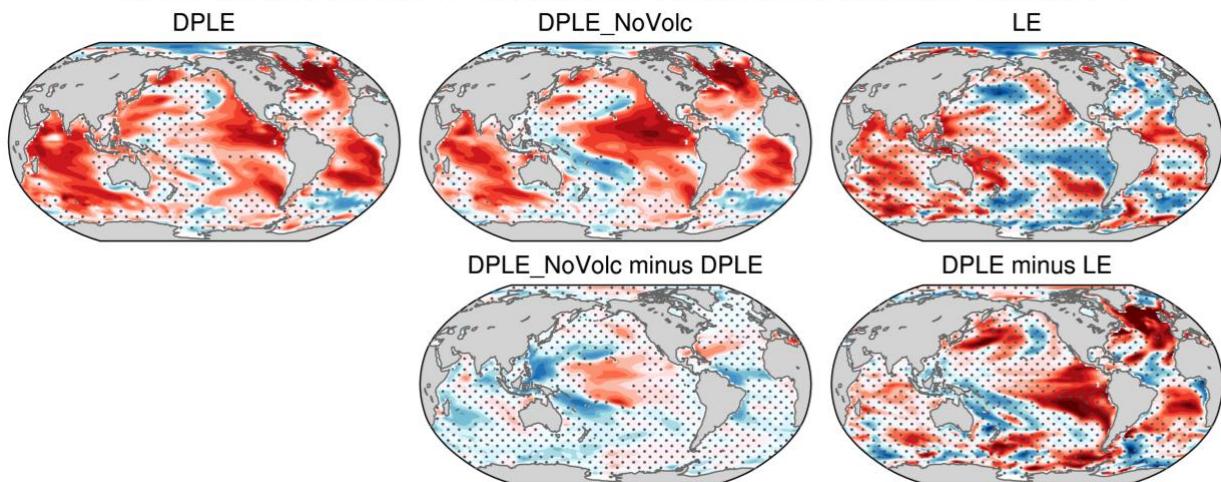


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89 **Fig. S12 Evaluation of SST initial conditions in FOSI** (top left) Correlation, (top right)
90 standardizes Root Mean Square Error (RMSE), and (bottom right) RMSE maps of SST in
91 November in FOSI compared to ERSSTv5 during 1954-2015.

ACC of annual mean SST, FY1-10, non detrended, verification data: FOSI 1955-2015



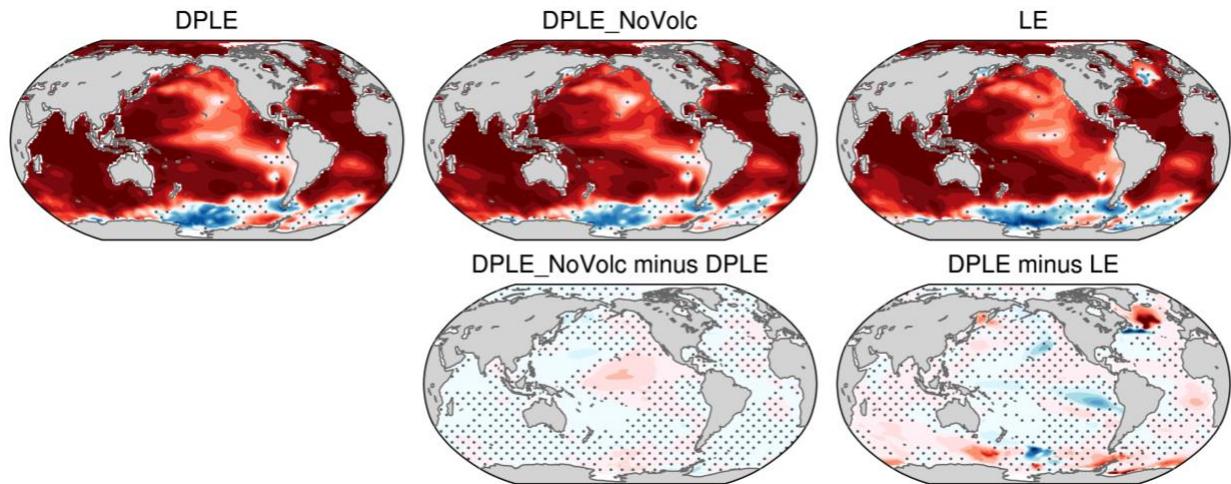
ACC of annual mean SST, FY1-10, quadratically detrended, verification data: FOSI 1955-2015



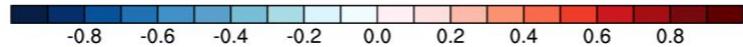
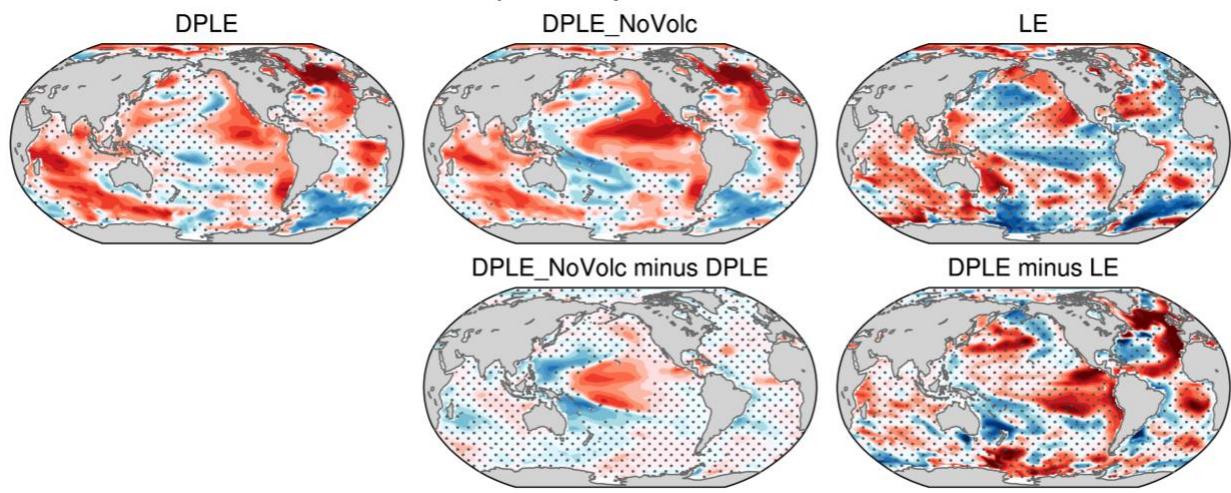
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Fig. S13 As in Fig. 2a–e in the main text, but for skill evaluation for the global SST relative to
FOSI.

ACC of annual mean SST, FY1-10, non detrended, verification data: ERSSTv5 1955-2022



ACC of annual mean SST, FY1-10, quadratically detrended, verification data: ERSSTv5 1955-2022



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97 **Fig. S14** As in Fig. 2a–e in the main text, but for skill evaluation for the global SST relative to ERSSTv5.