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**A New Robust Frontal Disturbance Index of the Oyashio Extension Sea Surface
Temperature Front.**

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35 **Abstract**

36 The Oyashio Extension (OE) frontal zone in the Northwest Pacific Ocean is associated with
37 strong gradients of sea-surface temperature (SST) and salinity. Like other frontal zones, the
38 OE front enhances baroclinicity and anchors the storm tracks; thus, changes in its position
39 and strength may impact atmospheric variability. North-south shifts in the OE front are often
40 defined using the leading principal component for the latitude of the absolute maximum SST
41 gradient in the Northwest Pacific (145-170°E)-the so-called Oyashio Extension Index (OEI).
42 We show that the OEI is sensitive to the choice of SST dataset used in its construction, and
43 that regressions of atmospheric fields onto the OEI also depend on the choice of SST
44 datasets, leading to non-robust results. This sensitivity primarily stems from the fact that the
45 longitudinal domain used to define the OEI includes a region with parallel or indistinct
46 frontal zones in its central section (155-164°E), leading to divergent results across datasets.
47 In particular, we advise against the use of ERA5 SST data for such analyses, as it is a clear
48 outlier. To circumvent the robustness issue, we introduce a new index that considers the
49 degree of continuity of the SST front across this central section - the Frontal Disturbance
50 Index (FDI). We show that the FDI produces more robust results on the influence of the OE
51 front on air-sea interactions and associated high-frequency storm-track metrics than the
52 conventional OEI. There are significant asymmetric associations between the FDI and storm-
53 track metrics dependent on the sign of the FDI.

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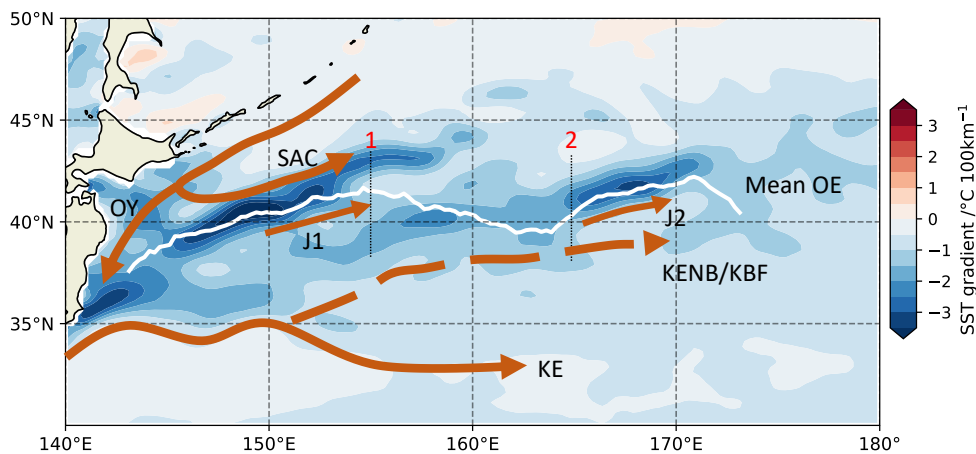
55 **Significance Statement**

56 In this study we aim to understand how the choice of dataset may influence the interpretation
57 of interactions between the ocean and the overlying atmosphere near sea-surface temperature
58 (SST) fronts. We find that using different SST datasets affects the results, due to slight
59 differences in the representation of the location of the maximum SST gradient. As a response
60 to this we develop a new index which relates to the degree of disturbance of the SST front.
61 This produces results that are more consistent across the different datasets. We also identify
62 Some possible links between the frontal disturbance and the presence of ocean eddies. We
63 advise that the sensitivity to dataset choice is given due consideration in regions near SST
64 fronts.

65

66 **1.Introduction**

67 Oceanic western boundary currents (WBCs) transport significant quantities of heat eastwards
68 and polewards in both the North Atlantic and Pacific Oceans. In the Atlantic the WBC is the
69 Gulf Stream, while in the Pacific the configuration is different: to the south is the Kuroshio
70 current, while to the north and forming part of the subpolar gyre, is the Oyashio current (Qiu,
71 2019). Both currents turn eastwards away from the coast of Japan and into the Pacific basin
72 where they are known as the Kuroshio Extension (KE) and Oyashio Extension (OE; also
73 sometimes referred to as the subarctic current or front), located at around 35°N and 41°N
74 respectively (Kwon et al., 2010). The OE is associated with strong gradients of sea-surface
75 temperature (SST) and salinity, whereas the KE is more clearly defined by a gradient in sea-
76 surface height (SSH) (Qiu et al., 2017). These features are shown schematically in Figure 1.
77 The region is very complex, with a number of diverging and converging currents between the
78 two extensions (Kida et al., 2015; Yasuda, 2003)



79

80 **Figure 1.** Schematic of the location of fronts referred to in the text. KE: Kuroshio Extension;
81 KENB/KBF: Kuroshio Extension Northern Branch/Kuroshio Bifurcation Front; OY: Oyashio
82 Current; SAC: Subarctic Current; OE: Oyashio Extension (143-173°E, shown in white); J1, J2:
83 Isoguchi jets. Background field is the mean December-March (DJFM) SST gradient from the
84 Reynold optimally interpolated (OI) SST dataset. (SST is not detrended). Meridional lines (1
85 and 2) mark the longitudinal segment within the OE used to calculate the Frontal Disturbance
86 Index (FDI: 155-164°E). Data are not detrended.

87

88 The strong meridional gradients of SST in the OE region may act to enhance baroclinicity and
89 anchor the storm track in the overlying atmosphere (Hoskins and Valdes, 1990; Nakamura et
90 al., 2008) and have been the focus of numerous observational and modelling studies concerning
91 air-sea interactions (Kwon et al., 2010; Frankignoul et al., 2011; Taguchi et al., 2012; Smirnov
92 et al., 2015; Révelard et al., 2016; 2018). Air-sea heat fluxes associated with mesoscale air-sea

93 interaction are robust in the vicinity of WBCs (Seo et al., 2023). The SST signal from
94 mesoscale processes such as eddies and SST fronts modify the surface turbulent heat and
95 momentum fluxes and cause local responses in the marine atmospheric boundary layer (Small
96 et al., 2008). This in turn drives a non-local response in the storm-track (e.g. Czaja et al., 2019;
97 Seo et al., 2023). A poleward decrease in sensible heat flux across the frontal zone sustains
98 the strong near-surface baroclinicity against the relaxing effect of strong poleward eddy heat
99 transport (Sampe et al., 2010).

100

101 It is important to better understand the nature of SST variability and associated air-sea
102 interactions along oceanic frontal zones, to improve the process level understanding of ocean-
103 to-atmosphere feedbacks as well as the performance of model simulations. Crucial questions
104 are the extent to which air-sea interactions over the OE region influence the wider atmospheric
105 circulation, and how this depends on the sharpness of the SST gradient, location of the gradient
106 and magnitude of the associated SST anomalies more generally (Small et al., 2019). Many
107 modelling studies (e.g. Smirnov et al., 2015; Ma et al., 2017; Kuwano-Yoshida and Minobe,
108 2017; Yook et al., 2022) impose observed SST anomalies in the Kuroshio-Oyashio Extensions
109 (KOE) region in an atmospheric model to investigate causal linkages. The atmospheric
110 response may depend not only on the spatial resolution of the model, but also on that of the
111 imposed SST anomalies. Only when the model has sufficient horizontal resolution can the full
112 impact of mesoscale forcing by SST fronts on the storm track be correctly simulated (e.g.
113 Smirnov et al., 2015; Ma et al., 2017).

114

115 To address these questions concerning air-sea interactions, there must be high confidence in
116 determining the location and shifts in these SST frontal zones, and the nature of the associated
117 SST anomalies. Frankignoul et al. (2011) developed an OE Index (OEI) based on the location
118 of the maximum SST gradient in the OE region (145-170°E), which has been used in a number
119 of subsequent studies (e.g. Kwon and Joyce, 2013; Smirnov et al., 2015; Qiu et al., 2017, Wu
120 et al., 2018; Yao et al., 2018a,b). Frankignoul et al. (2011) identified that north-south shifts in
121 the SST front were associated with large-scale atmospheric responses up to three months later.
122 Subsequent work (Qiu et al., 2017) concluded that the western (145-153°E) and eastern (153-
123 173°E) sections of the OEI were in fact uncorrelated on a synchronous basis over a range of
124 different timescales, although lagged relationships did occur. The different sections of the front
125 were driven by different physical mechanisms (Wu et al., 2018), and were associated with
126 different SST anomaly patterns. It therefore makes sense to treat the variability of the two

127 sections of the front separately. Other studies identify SST frontal indices based on simple
128 regional anomalies, although these are often applied to the general KOE region (e.g. 36-42°N,
129 140-171°E) and may provide different information about air-sea interactions that are not
130 necessarily connected to shifts in SST fronts (e.g. Taguchi et al., 2012; Wills and Thompson,
131 2018).

132

133 The reliability of analyses of SST-front-driven air-sea interactions depends on the ability of
134 SST datasets to accurately represent the SST front. New high-resolution gridded SST datasets
135 are available, with horizontal resolutions commonly of 0.25° in latitude and longitude or
136 higher. The credibility of these SST products depends upon the availability of observations and
137 the gridding procedure used (Huang et al., 2021). Gridded SST datasets capture well large-
138 scale modes of variability such as El-Nino-Southern Oscillation (ENSO) with high correlations
139 between time series derived from different datasets (Yang et al., 2021). However, for assessing
140 air-sea interactions over the WBCs and associated SST fronts, there is considerable variation
141 between datasets and the sharpness of a front in the dataset is not necessarily proportional to
142 the grid resolution used (Martin et al., 2012; Fiedler et al., 2019). These differences are related
143 to distinctive retrieval and interpolation methods and interpolation grid-size, and bias-
144 correction of input data (Yang et al., 2021).

145

146 We are therefore motivated to calculate the OEI for a range of SST datasets to determine first,
147 their level of agreement and second, to identify whether the differences impact significantly on
148 the interpretation of air-sea interactions. We also investigate whether any discrepancies in the
149 OEI have any physical basis, and the significance of this for future studies. We find that the
150 OEI interaction with atmospheric variables is dataset dependent. This leads us to develop a
151 new index, the Frontal Disturbance Index (FDI), which, we think, is more robust to variations
152 between datasets. The data used in the study are described in section 2, and methods are
153 explained in section 3. Section 4 presents our results, and section 5 is a discussion and summary
154 of our findings.

155

156 **2.Data**

157 In assessing air-sea interactions associated with SST fronts, reliable high-resolution SST
158 datasets, which resolve mesoscale processes are required. One option is to obtain these from
159 the newest generation of gridded observational datasets, with increased temporal and spatial
160 resolution. The National Oceanic and Atmospheric Administration (NOAA) optimum-

161 interpolated (OI) SST version 2.1 dataset (Reynold et al., 2007; Banzon et al., 2016; Huang et
162 al., 2020) is available at daily resolution on a 0.25° grid from 1981 to the present for the
163 AVHRR-only product. The Operational Sea Surface Temperature and Sea Ice Analysis
164 (OSTIA) dataset (Donlon et al., 2012; Good et al., 2020) is available from October 1981
165 onwards at a daily resolution on a 0.05° grid. In addition, we use the Group for High-Resolution
166 SST Multi-Product Ensemble (GMPE, Martin et al., 2012; Fiedler et al., 2019) analysis for
167 1981 to 2016 at daily resolution on a 0.25° grid. The GMPE uses an ensemble of six high-
168 resolution products (including OSTIA and OI; Fiedler et al., 2019) and takes the ensemble
169 median value for each grid box, having regridded the data to a common grid. Details of the
170 method are described by Martin et al. (2012). We also compare these products to the SSTs in
171 the ERA5 reanalysis (Hersbach et al., 2020), available on a 0.25° grid with an hourly timestep
172 from 1940 onwards. ERA5 uses Hadley Centre Ice and Sea Surface Temperature version 2.1.0
173 (HadISST2.1.0) for the period to 2007 (at 5-day and 1° resolutions; J.J. Kennedy, pers.comm),
174 and OSTIA thereafter. It should be stressed that none of these datasets is independent, as they
175 use many of the same satellite, and in-situ data sources; however they are selected as being
176 representative of typical datasets that may be used in the analysis of air-sea interactions. We
177 calculate monthly means of daily data for the common period January 1982 to December 2016,
178 regridding to a common 0.25° grid. The OEI and FDI are calculated separately for each SST
179 dataset (see section 3).

180

181 Atmospheric and surface flux variables (sea-level pressure (SLP), meridional wind, total
182 precipitation, latent and sensible heat fluxes, vertical velocity (omega)) are obtained from the
183 ERA5 reanalysis, to assess the impact of different OEI and FDI indices on storm-track
184 variability. Sea-surface height (SSH) data are obtained by using the sea-level anomaly dataset
185 from the Copernicus Marine Environment Monitoring Service (CMEMS). This is an altimeter
186 satellite product available as gridded data at 0.25° and daily resolution, from 1993 (doi:
187 10.48670/moi-00148). For SSH we use the period 1993-2016, to ensure a common period with
188 other datasets.

189

190 **3. Methods**

191 **3.1 Definition of the Oyashio Extension Index (OEI)**

192 Following Frankignoul et al. (2011), we calculate the OEI as the monthly standardised
193 principal component (PC) monthly timeseries for the first empirical orthogonal function (EOF)

194 of the latitude of the absolute maximum meridional SST gradient for the September-to-April
 195 period, based on the monthly SST data. This period is chosen to avoid the summer season,
 196 because the summer SST gradient has different characteristics. We identify the latitude of the
 197 maximum SST gradient at each longitude over the OEI region at each timestep, but restrict the
 198 EOF calculation domain to the eastern part of the region (35-47°N, 153-173°E) following Qiu
 199 et al. (2017). We detrend the latitude of maximum SST gradients using a third order polynomial
 200 fit for the 1982-2016 period, and the mean seasonal cycle is removed by subtracting the
 201 climatological monthly means prior to the calculation of the EOF.

202

203 Based on the monthly OEIs calculated from each dataset following the above procedure, three
 204 versions of the OEI are calculated for the December-March seasonal window: 1) monthly; 2)
 205 seasonal mean; and 3) monthly intra-seasonal (anomalies from the seasonal mean for each
 206 year). These indices allow us to compare how similar the indices are at different temporal
 207 resolutions. We also calculate an extended monthly series from September to April. The OEIs
 208 from different datasets for each of these versions are compared by computing pair-wise
 209 correlation coefficients and a time series of average pair-wise differences (the “Difference
 210 index”) is calculated for the September-April monthly timeseries.

211

212 3.2. Definition of the Frontal Disturbance Index (FDI)

213 The OE SST front is relatively weak and diffuse in the central portion of the domain (Fig. 1).
 214 To assess the extent to which the location of OE front departs from the climatology across this
 215 section, we compute a “Frontal Disturbance Index” (FDI) as follows. First, we calculate the
 216 detrended (third-order polynomial fit) standardised anomaly of the latitude of the SST front F
 217 as the latitude of the maximum SST gradient (ϕ) as a function of longitude (λ) and time
 218 ($t=1 \dots N$) within 155-164°E:

$$219 \quad F_{t,\lambda} = \frac{\phi_{t,\lambda} - \bar{\phi}_\lambda}{\sqrt{\frac{1}{N-1} \sum_{t=1}^N (\phi_{t,\lambda} - \bar{\phi}_\lambda)^2}} \quad (1)$$

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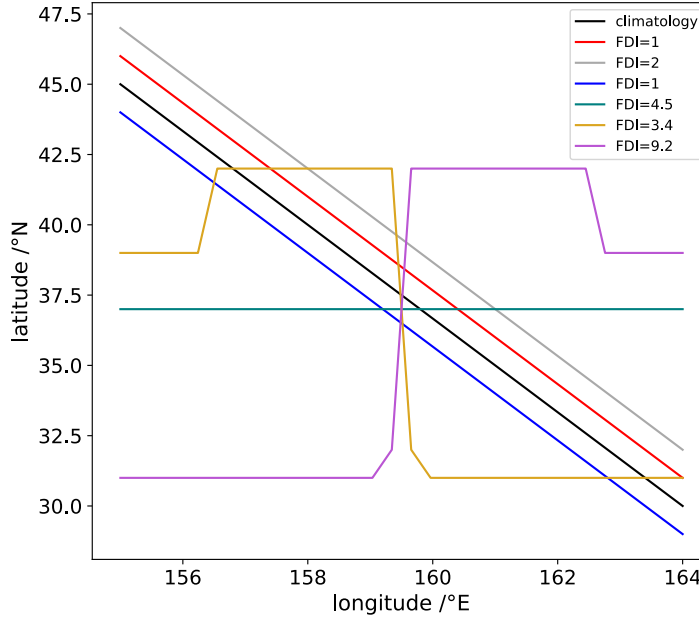
221 where the overbar denotes time mean. Then, we find the root mean square deviation of these
 222 standardised anomalies with respect to longitude ($l=1 \dots M$):

$$223 \quad FDI_t = \sqrt{\frac{1}{M} \sum_{\lambda=1}^M F_{t,\lambda}^2} \quad (2)$$

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Higher FDI values indicate a higher overall departure from the climatological time-mean. As constructed, the FDI captures both absolute departures from the time mean latitude, and also the extent to which the maximum SST gradient makes large latitudinal jumps between adjacent longitudes.

A schematic diagram of the FDI calculated for synthetic data is shown in Figure 2. For this example, the climatology has an FDI value of zero, the minimum possible. SST gradient locations are chosen to show that the FDI value is proportional to the absolute magnitude of the mean displacement from climatology, not the sign (red and blue lines have equal FDI values even though they are on opposite sides of the climatology). As distance from climatology increases, so does the FDI (gray line). While the green line is purely zonal in orientation, it has an FDI of 4.5 as it intersects climatology at an angle, with increasing differences further from the intersection. The two stepped lines are the reverse of each other. However, their FDI values are different, as with the orange line the step down is broadly aligned with climatology whereas in the purple line, as climatological values decrease eastwards, the step broadly increases in latitude. In the SST datasets analysed here, the range of FDI values is from around 0.3 to 1.9. We also calculate a mean FDI, which is the ensemble mean of the FDI values calculated for different datasets at a given monthly timestep. For use in asymmetric regression, we remove the climatological monthly mean FDI from the timeseries, thus the large negative FDI values indicate the frontal positions close to climatology.



246

247 **Figure 2.** Diagram of synthetic data simulating different locations of maximum SST gradients,
 248 over the longitude and latitude range of the central section of the OE (155-164°E). The
 249 synthetic climatological maximum SST gradient is shown by the bold black line, and five
 250 different synthetic gradient locations are shown, together with the FDI value for each.

251

252 3.3. Other Calculations

253 To assess any physical mechanisms that might be linked to the FDI, we isolate oceanic
 254 mesoscale features (including coherent eddies) in the region 150-170°E, 30-50°N. We use a
 255 two-dimensional fast Fourier transform (FFT) spatial filter to isolate high and low
 256 wavenumbers in the SST data. We filter daily data, using a filter length-scale of 420km as a
 257 cutoff, (wave number equal to 0.0024 km^{-1}) to separate eddy length-scales from larger scales
 258 and then calculate the monthly standard deviation of the resulting data. The highpass filter
 259 isolates the mesoscale eddies, but produces a field with a lot of noise. To identify any large-
 260 scale patterns in the mesoscale eddies, we additionally apply a FFT lowpass spatial filter with
 261 the same cutoff as the highpass filter to the monthly standard deviation fields of the highpass
 262 data. For full details of the method used, see Sroka et al. (2022). For comparison we also
 263 calculate daily surface Eddy Kinetic Energy from the SSH data according to:

$$264 \quad EKE = \frac{1}{2}(u_g'^2 + v_g'^2) = \frac{1}{2} \left[\left(-\frac{g}{f} \frac{\partial h'}{\partial y} \right)^2 + \left(\frac{g}{h} \frac{\partial h'}{\partial x} \right)^2 \right], \quad (3)$$

265

266 where u_g' and v_g' are the zonal and meridional components of the geostrophic current anomaly
 267 respectively, f is the Coriolis parameter, g is the gravitational acceleration, h' are the SSH

268 anomalies and y and x are distances along the latitudinal and longitudinal directions
269 respectively.

270

271 We calculate the monthly standard deviation of 8-day highpass-filtered daily data of surface
272 turbulent heat flux (THF, the sum of sensible and latent heat fluxes) and 500hPa vertical
273 velocity (ω) by applying a 4-point highpass Butterworth filter to the daily data, to isolate
274 variability at the synoptic timescale. These fields can give an indication of storm-track activity,
275 increased variance being associated with passage of low-pressure systems, where both
276 enhanced positive and negative heat fluxes and vertical velocity can occur in different locations
277 within the same system, associated with warm and cold sectors and fronts. We also calculate
278 indicators of surface storm-tracks, using an alternative highpass filtering approach involving
279 daily differencing (Wallace, 1998). We apply this to 850hPa meridional wind and total
280 precipitation. In addition, the Eady Growth Rate (EGR) at 800hPa is calculated according to:

281
$$EGR = -0.31 \frac{g}{N\theta_o} \frac{\partial \theta}{\partial y} \quad (4)$$

282 where N is buoyancy frequency, θ is potential temperature and θ_o is the climatological monthly
283 mean temperature (e.g., Small et al. 2014). The EGR is an important measure for identifying
284 baroclinic eddy development (e.g. Hoskins and Valdes, 1990).

285

286 We identify large-scale air sea interactions associated with the OEI and FDI by regressing the
287 different atmospheric variables including storm-track metrics from ERA5 (section 2) on the
288 monthly timeseries. We use both conventional symmetric linear regression and asymmetric
289 regression to accommodate potential non-linear associations with respect to the sign of the
290 index (e.g. Révelard et al., 2016). The asymmetric regression method is described in detail in
291 Frankignoul and Kwon (2022). Negative and positive values of the index (recall the FDI is
292 adjusted by removal of the climatological mean, creating positive and negative values) are
293 regressed separately against the relevant time steps of the cubic-detrended anomaly field,
294 having first removed the time mean for negative and positive index values, separately, from
295 each set of data to provide an unbiased estimate. Statistical significance for regressions is
296 determined using the Wald test (similar to the Student's t-test; Wald, 1943) and we present
297 results for two levels of significance ($p < 0.1$, $p < 0.2$). We apply the False Discovery Rate (FDR;
298 Benjamini and Hochberg, 1996; Wilks, 2015) to compensate for spatial autocorrelation and
299 multiple testing.

300

301 **4.Results.**

302 **4.1 The Sensitivity of the OEI to Choice of Dataset.**

303 Correlations between the OEIs show considerable variation between dataset pairs and depend
304 on the temporal window and resolution used (Table 1).

correlation	SONDJFMA separate months	DJFM separate months	DJFM Seasonal mean	DJFM subseasonal anomalies
ERA5 vs. OI	0.72	0.62	0.69	0.49
ERA5 vs. GMPE	0.71	0.61	0.71	0.46
ERA5 vs. OSTIA	0.71	0.57	0.75	0.24
OI vs. GMPE	0.81	0.78	0.88	0.58
OI vs. OSTIA	0.80	0.72	0.77	0.53
GMPE vs.OSTIA	0.78	0.72	0.86	0.41

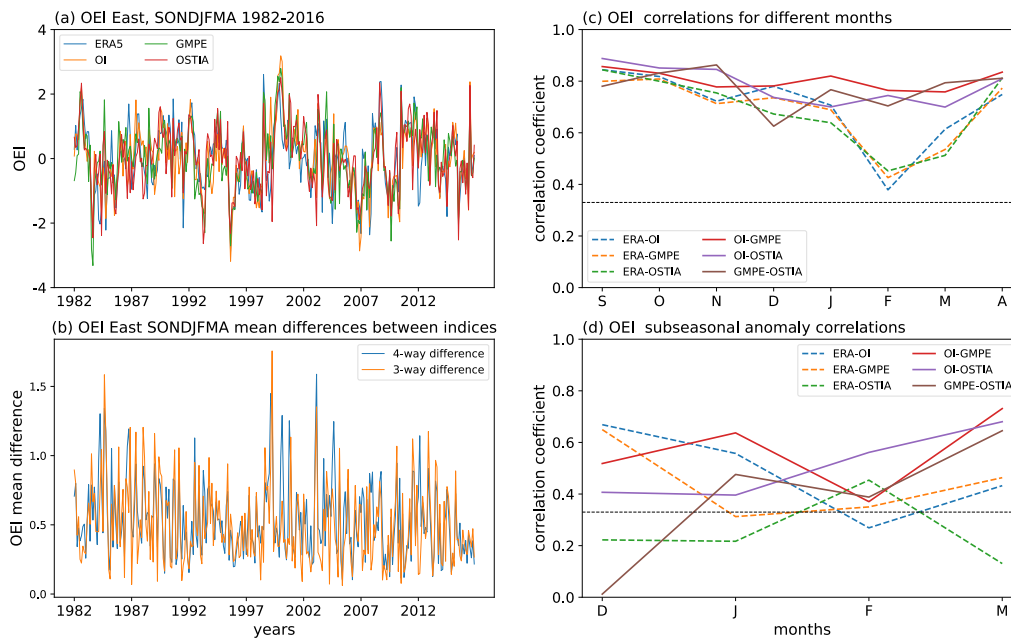
305 **Table 1.** Pearson correlations between the PC-based OEI timeseries for different SST datasets,
306 and for different temporal resolutions. All correlations are calculated for 1982-2016. All
307 correlations are significant ($p < 0.05$).

308

309 The correlations are higher for the September-April monthly resolution timeseries than for the
310 extended winter (DJFM) monthly series, indicating weaker correlations in the winter months.
311 Correlations for DJFM seasonal means are quite high (0.69-0.88), while those for subseasonal
312 anomalies are much lower (0.24-0.58). The correlations for time series of separate DJFM
313 months lie somewhere in between. Correlations with ERA5 and other datasets are generally
314 lower than those between other dataset pairs.

315

316 The September-April (SONDJFMA) OEI with monthly resolution shows good agreement
317 across datasets at multiannual timescales (Figure 3a), while the Difference Index shows that
318 there can be considerable disagreements on monthly timescales (Figure 3b). Over the
319 September to April window, a seasonal cycle in correlations between ERA5 and the other
320 datasets is evident (Figure 3c) with lower correlations in the winter months (generally February
321 and March). The lower ERA5 correlations in February and March are also present in the
322 subseasonal anomalies, although here the correlations are even lower, with increased noise in
323 the datasets at subseasonal timescales (Figure 3d). These correlation statistics suggest that the
324 OEI may be most suitable for use with seasonal means for calculating interannual variability.



326

327 **Figure 3** (a). The OEIs (eastern section, 153-173°E) for September to April with monthly
 328 resolution based on the 4 different SST datasets, and (b) the mean absolute difference between
 329 the indices, calculated between all indices (4-dataset difference) and without ERA5 (3-dataset
 330 difference). (c) Interannual correlations between OEIs for each month in the window
 331 September - April based on different pairs of SST datasets. (d) As in (c) but for the subseasonal
 332 anomalies in DJFM. In c) and d) correlations between ERA5 and other datasets are shown as
 333 dashed lines and the horizontal dashed lines denote the significance threshold for $p < 0.1$.

334

335 When atmospheric and SST fields are regressed on these different OEIs, the results are
 336 inconsistent across the datasets, leading to concerns regarding interpretation when a single
 337 dataset is used (Figure S1). When OEI timeseries and SST datasets are swapped, so that for
 338 example the OI SST is regressed on the ERA5 OEI, the same spatial patterns of regression
 339 coefficients are obtained as that when regressing the ERA5 SST on the ERA5 OEI. This
 340 suggests that inconsistencies arise from the OEIs.

341

342 From the results shown in Figure 3, ERA5 seems to be an outlier in that it disagrees with other
 343 SST datasets considered. Thus, we do not consider this SST product further in the subsequent
 344 analysis.

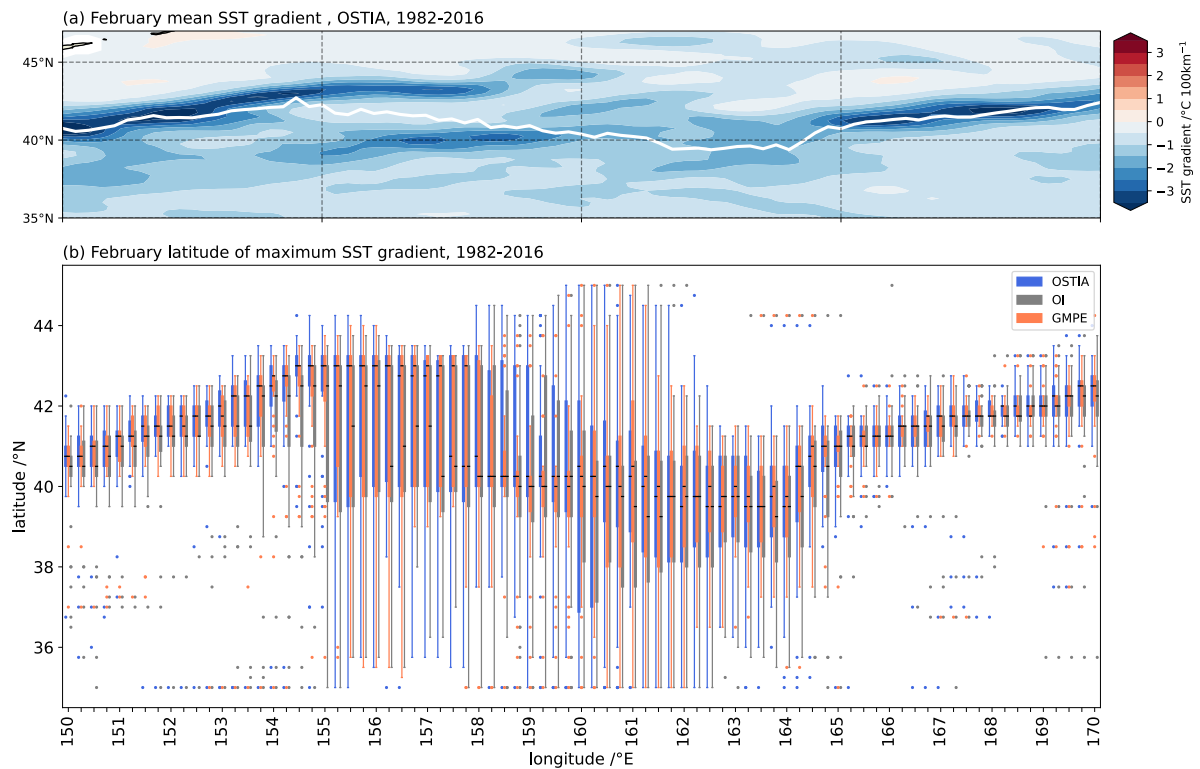
345

346 4.2 Reasons for OEI Discrepancies

347 Here we investigate the differences in the OEI across datasets to identify their origin. Our focus
 348 is on the spatial structure of SST gradients within the OE region.

349

350 The SST gradient pattern in the OE region is complex. As an example, the February-mean SST
351 gradient pattern for the OSTIA dataset is shown in Figure 4a. The region does not contain a
352 single continuous front: there are parallel fronts, single well-defined fronts and regions where
353 the front is poorly defined. Other datasets have very similar patterns (Figure S2) and those for
354 other months are qualitatively similar (not shown).



355

356 **Figure 4.** (a) Spatial pattern of the February mean SST gradient from OSTIA for 1982-2016.
357 White line shows the February climatological absolute maximum SST gradient. (b) Box and
358 whisker plots showing the February latitudinal distribution of the maximum poleward absolute
359 SST gradient at each longitude, for each dataset for 1982-2016 (OSTIA in blue, OI in gray and
360 GMPE in orange). The central box at each longitude shows the interquartile range (IQR), the
361 horizontal black line indicates the median. The whiskers extend from each box by 1.5 times
362 the IQR and dots indicate values that occur outside these ranges.

363

364 The latitudinal occurrences of absolute maximum poleward SST gradients shown for February
365 in Figure 4b illustrate these distinct regions. Within 150-155°E and 165-170°E there are strong,
366 well-defined SST gradients. These clearly defined SST fronts to the west and east correspond
367 to the locations of the Isoguchi jets (Isoguchi et al., 2006; Kida et al., 2015; J1 and J2 in Figure
368 1). These quasi-stationary geostrophic jets transport warm water polewards. This explains their
369 consistent representation amongst the datasets and the relatively narrow interquartile ranges

370 (IQR) in Figure 4b. However, within 155-165°E, the pattern of SST gradients is more complex.
371 Two parallel SST gradient fronts are evident from 155-160°E (one near 40°N, and the other
372 near 43°N (Figures 4a and S2). The broad IQRs on the boxplots here indicate sampling of the
373 maximum SST gradient from both regions of strong SST gradients (figure 4b), with datasets
374 showing different preferred latitudes at different longitudes and times. While OSTIA and
375 GMPE show a skewed distribution with more frequent sampling of the northern front, the
376 median value for OI is located further south, particularly between 156-157°E, indicating that
377 the maximum SST gradient occurs more frequently along the more southern SST gradient
378 region in OI. At around 159°E, OSTIA has a much wider IQR than either OI or GMPE.
379 Between 160-164°E there is a more diffuse front, with fragmented sections of stronger and
380 weaker gradients. In February this zone of weak overall gradients is broadest latitudinally and
381 may contribute to the low correlations in OEI timeseries in February (Figure 3c,d). Some of
382 the differences between the OEIs arise from the central section: either slight differences in the
383 representations of the relative strengths of the parallel fronts in its western half means that
384 different latitudes are selected by the datasets, or over the diffuse, shallow front in the eastern
385 half, small differences in gradient strength could result in large latitudinal discrepancies
386 between datasets. Other months are qualitatively similar and display the same regions of
387 discrepancies (not shown).

388

389 **4.3 OE Variability and Frontal disturbance for 155-164°E**

390 We now examine the central section of the OE SST front, using the FDI calculated over 155-
391 164°E. This longitude range comprises just under half the length of the OE used to calculate
392 the Eastern OEI (153-173°E). Recall that a high FDI indicates the OE front has a large
393 departure from climatology, whereas the smaller the value, the closer the front is to
394 climatology. The correlations between the GMPE and other FDI timeseries from different
395 datasets, at different temporal resolutions, are not as strong as those obtained from the OEI,
396 except for the DJFM subseasonal anomalies which are of similar magnitude. (Table 2,
397 compared with Table 1). This may be a consequence of the methodology used in constructing
398 the GMPE: selection of the median value from an ensemble at each grid point may not reflect
399 the actual disturbance of the front. Correlations between the OI and OSTIA FDI are of similar
400 magnitude to those of the OEI (greater in the case of subseasonal anomalies) and the
401 correlations for individual months are the lowest in December-April (Figure S3).

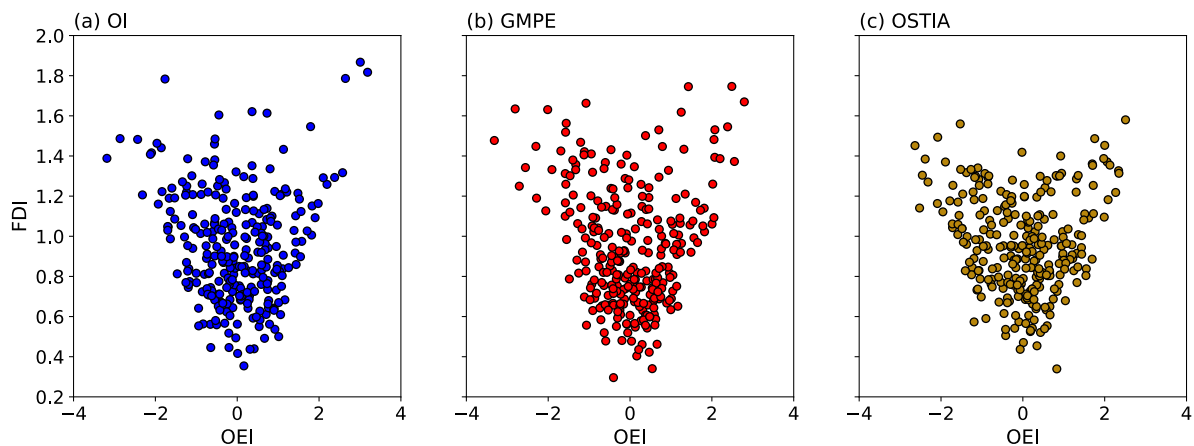
correlation	SONDJFMA separate months	DJFM separate months	DJFM Seasonal mean	DJFM subseasonal anomalies
OI-GMPE	0.61	0.55	0.56	0.55
OI-OSTIA	0.76	0.69	0.67	0.55
GMPE-OSTIA	0.64	0.62	0.77	0.40

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Table 2. Pearson correlations between the FDI timeseries for 155-164°E for different datasets and timesteps. All correlations are over the 1982-2016 period and all correlations are significant ($p < 0.05$).

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During September-April at monthly resolution, the FDI shows no significant ($p < 0.1$) correlations with the OEI in any of the datasets. However, if the OEI and FDI are partitioned based on the negative and positive OEI phases a different picture emerges. The positive phases of the OEI are positively correlated (OI: 0.54; GMPE: 0.59; OSTIA: 0.52) with the FDI, whereas for the negative phases of the OEI, they are negatively correlated (OI: -0.47; GMPE: -0.54; OSTIA: -0.50) with the FDI. These results explain why the correlations are negligible when the full timeseries are considered, but also identify a moderate association between poleward shifts (OEI) and increased frontal disturbance (FDI) in the positive phase. When the OEI is negative, a southward shift is also associated with a more disturbed front (a more positive FDI). The FDI increases as the OE front moves away from the climatological location in either direction. The relationship between the OEI and FDI is summarised in Figure 5.



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Figure 5. Scatterplots of the monthly OEI against monthly FDI for September-April, for (a) OI (b) GMPE and (c) OSTIA datasets, 1982-2016.

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In February, of the 12 years with the lowest OEI Difference Index, six have a low FDI, and one has a high FDI. Conversely, when the OEI Difference Index in February is high, three of the 12 years have a low FDI and seven have a high FDI. This makes sense as a broken, less

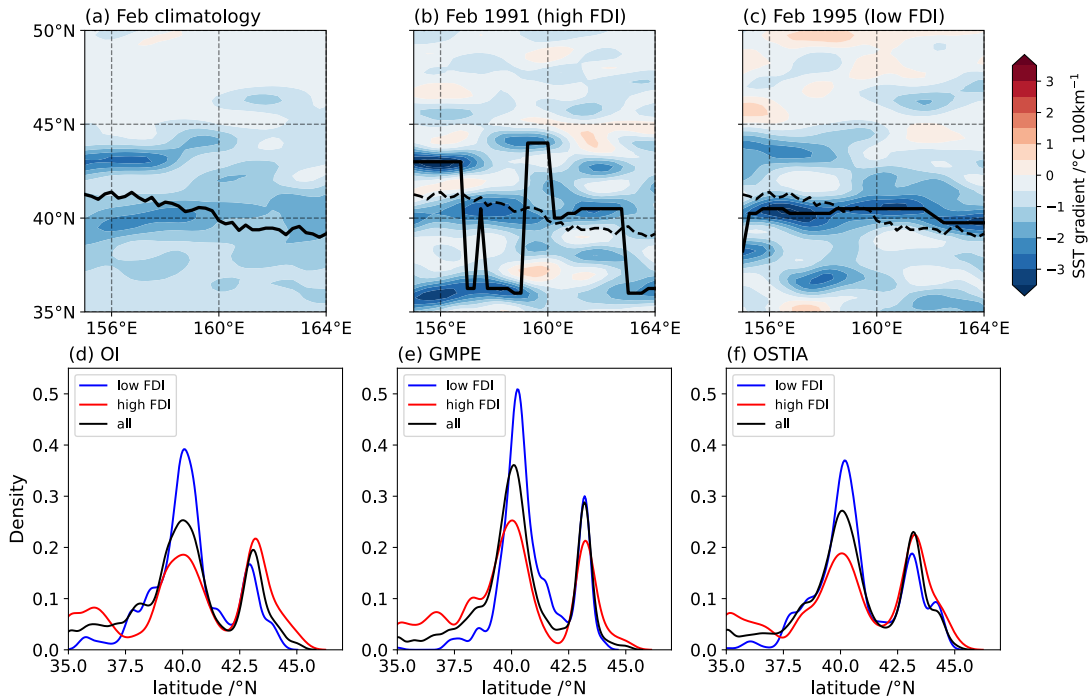
425 well-defined front may well be detected more ambiguously in different datasets. Additional
426 contributions to the Difference Index come from the more well-defined regions of the front,
427 where differences still occur for each timestep.

428

429 Using the OI SST dataset and considering the SST gradients in February as an example, the
430 FDI is high in the year 1991 (1.25) and low in 1995 (0.42) (Figure 6). In Figure 6a, the
431 climatological mean for the locations of the maximum SST gradients (black curve) does not
432 coincide with the climatological February-mean for the SST gradient field (shading). In the
433 west it lies between the two regions of strong poleward SST gradients, a consequence of the
434 average location reflecting fluctuations in the relative strength of the northern and southern
435 SST fronts. In 1991, large sections of the maximum SST gradient are located well to the north
436 and south of the climatology (Figure 6b), with the maximum around 35°N likely associated
437 with the KE. Such a large overall disturbance results in a high FDI in 1991. In contrast, in 1995,
438 the maximum SST gradients are close to but either side of the climatological values, with an
439 overall more zonal location and a low FDI.

440

441 A summary of the latitudinal distributions (density) of the absolute maximum SST gradients
442 for all Februarys (Figure 6d-f) shows that when the FDI is high (red), the distribution has a
443 greater spread, with higher and lower latitude values in the tails; whereas for low FDI years
444 (blue), the distribution has increased frequency around 40°N. High FDI months sample the
445 maximum SST gradients from higher or lower latitudes more frequently, with fewer
446 occurrences at around 40°N.



447
 448 **Figure 6.** February-mean poleward SST gradient (color shading, °C per 100km) for (a)
 449 February climatology 1982-2016, (b) February 1991 (a high FDI case) and (c) February 1995
 450 (a low FDI case) from the OI SST dataset. In (a), the locations of the maximum absolute SST
 451 gradients are shown with a black solid line which is drawn as black dashed lines in (b) and (c).
 452 Data are not detrended in (a–c). (d–f) Kernel density estimates of the distribution for latitudes
 453 of the February maximum absolute SST gradients, at each longitude and for each February in
 454 1982-2016 for (d), OI, (e) GMPE and (f) OSTIA. Blue (red) curves show the third of months
 455 with the lowest (highest) FDI, and black curve is for all the February months.
 456

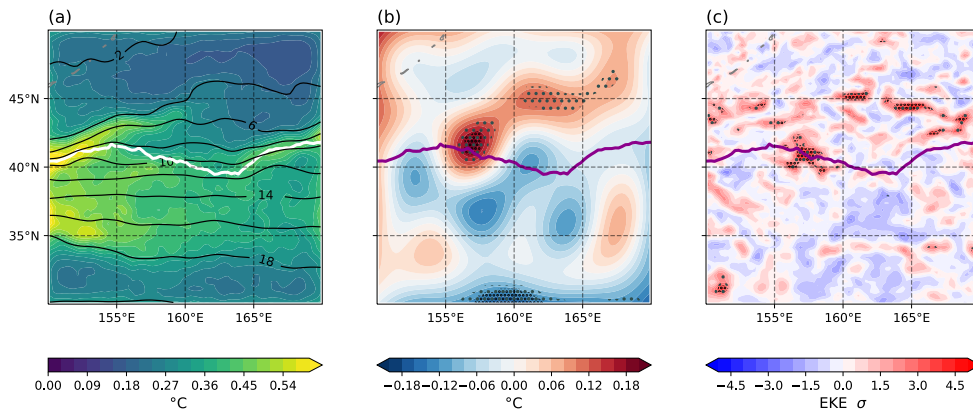
457 **4.4 Physical Factors Associated with the FDI.**

458 The FDI is moderately associated with the magnitude of the poleward SST gradient averaged
 459 over 39-41°N, 155-164°E. Specifically, correlations between the FDI and SST gradient are
 460 0.43(OI), 0.30 (GMPE) and 0.38 (OSTIA), based on monthly data during 1982-2016). All these
 461 values are highly significant ($p < 0.01$) and indicate that a stronger (more negative) poleward
 462 temperature gradient at 40°N is associated with a lower FDI, closer to climatology. This implies
 463 a stronger SST gradient at this latitude is more likely to be selected as part of the OE front
 464 defined along the maximum absolute SST gradient. Figure 6 provides an example of this: in
 465 the high FDI case (Figure 6b), there are regions of stronger (than climatology) positive
 466 poleward SST gradients to the north and south of 40°N, whereas in the low FDI case (Figure
 467 6c) the gradients along 40°N are the strongest in the domain. The probability density functions
 468 in Figure 6d,e,f reinforce this. There is a clear increase in occurrences of maximum SST
 469 gradients at around 40°N for low FDI months (blue lines), while for high FDI years, this
 470 frequency decreases, with increased frequency particularly at lower latitude (35-37°N, red

471 lines, in the KE region). There is a secondary frequency peak at around 43°N, where changes
 472 in frequency are dependent on dataset. The magnitude of the SST gradient at around 40°N
 473 explains only a part of the FDI, as it is likely to be a result of interactions between a range of
 474 variables related to local SST, SST gradients and SSH gradients, some of which may be non-
 475 linear.

476

477 We now consider whether mesoscale oceanic eddy activity has any influence on the FDI. The
 478 amplitude of mesoscale eddy activity is calculated from the monthly standard deviation of daily
 479 OI SST data that have been highpass-filtered by application of a spatial FFT filter (Section 3.3;
 480 Figure 7). There is high mesoscale eddy activity in the region between the KE and OE (Figure
 481 7a) (~35-41°N). In addition, there is increased eddy activity along the two quasi-stationary
 482 regions of strong SST gradient associated with the OE Front (150-160°E, 40-44°N, and 165-
 483 170°E, 40-43°N).



484

485 **Figure 7.** (a) OI SST monthly standard deviation of spatially high-pass filtered daily data
 486 averaged over DJFM, 1982-2016. Black contours show the DJFM mean SST. (b) Monthly
 487 standard deviation of daily spatially highpass filtered SST, with additional lowpass filter
 488 applied to the monthly standard deviations prior to regression, regressed against the OI FDI
 489 (for positive FDI months only). (c) monthly mean Eddy Kinetic Energy standardised anomalies
 490 regressed against the average FDI (positive regression only). Stippling indicates significance
 491 at $p < 0.1$ (fine black) and $p < 0.2$ (coarse gray) after the application of the False Discovery Rate.
 492 The monthly SST data are detrended prior to regression. The DJFM mean location of the OE
 493 is shown in white in (a) and magenta in (b) and (c).
 494

495 The FFT-filtered OI SST fields regressed onto the FDI for December-March results in
 496 significant increased mesoscale eddy energy in positive regression (Figure 7b) to the north of
 497 the climatological SST. The additional lowpass filtering cleans up the very noisy highpass-
 498 filtered fields. A similar pattern is observed using OSTIA data, although the field is noisier and
 499 results are not significant (not shown). However, if the regressions are repeated for December-
 500 January or January-February, significance is found using both OI and OSTIA (not shown; note

501 that we do not use GMPE for these results as the median method of calculation used for creating
502 GMPE may potentially have a smoothing effect on mesoscale features). A high FDI indicative
503 of a more disturbed maximum SST gradient, is associated with increased eddy activity to the
504 north. To confirm the association between mesoscale eddy activity to the north of the Oyashio
505 SST front and the FDI, we regress the eddy kinetic energy (EKE) monthly-mean standardised
506 anomalies against the average FDI (Figure 7c). In agreement with the results derived from
507 spatial highpass-filtered SST, the EKE from SSH indicates increased eddy activity to the north
508 of the SST front for a positive FDI. If the monthly standard deviation of standardised EKE
509 anomalies is regressed against the average FDI, a similar pattern emerges (not shown)
510 suggesting a shift in both the mean and spread of EKE with an increased FDI.

511

512 There is evidence of significant oceanic mesoscale eddy activity leading the FDI by one month
513 (not shown), further suggesting the mesoscale eddy activity is influencing the FDI. While the
514 FDI shows an association with SST mesoscale eddy activity, there is no significant association
515 with local unfiltered SST variability (not shown).

516

517 **4.5 Impacts of Changes in Frontal Continuity**

518 We now address whether the variability of the FDI is manifested in atmospheric fields over a
519 North Pacific domain defined by the region between 130-240°E and 30-65°N by regressing the
520 various storm-track metrics (highpass-filtered turbulent heat flux (THF) and 500hPa omega;
521 daily-differenced 850hPa meridional wind and total precipitation and 800hPa EGR) and SLP
522 against the FDI. We compare the results with analogous regressions based on the more familiar
523 OEI. We primarily examine significant regressions at one-month lag between the respective
524 FDI and OEI in January and February (JF) and the February and March (FM) atmospheric
525 fields, at monthly resolution. This time lag is chosen to capture the influence of the changes in
526 frontal disturbance or OE shift on the atmosphere, avoiding atmospheric influences on the
527 ocean which dominate at zero lag. Significant changes can also be observed at longer lags (not
528 shown); however we do not aim to be exhaustive here, focussing instead on the novel result
529 that the frontal disturbance of the central section of the OE is associated with significant
530 changes in atmospheric variables at one-month lag. We focus on a small number of metrics
531 below for clarity, and also average the indices across the different datasets, to reduce noise.

532

533 Symmetric and asymmetric regression results are summarised in Table 3, with statistical
534 significance at $p < 0.1$ and $p < 0.2$ indicated by dark and light blue shading, respectively. Recall

535 that for these regressions we remove the climatological mean FDI to create positive and
 536 negative values. It is notable that for the FDI, there are no significant negative results for the
 537 individual datasets, (i.e. when the fronts are closer to their climatological mean position).
 538 Similarly for the OEI, significances for positive regressions, when the front shifts to the north,
 539 are much more frequent than for negative regressions. In addition, for the FDI, significance is
 540 found for positive regressions of SST mesoscale eddy activity (Figure 7) and the storm-track
 541 metrics (Figure 9; Table 3) against the FDI, suggesting a possible causal link between SST
 542 mesoscale eddies and storm-track metrics a month later.

543

(a) FDI dataset JF	February-March atmospheric field																	
	THF SD highpass			500hPa omega SD highpass			850hPa v wind differences SD			Total Precip. differences SD			800hPa Eady Growth Rate			SLP		
	+	-	s	+	-	s	+	-	s	+	-	s	+	-	s	+	-	s
OI																		
GMPE																		
OSTIA																		
MEAN																		
Agreement score	0	0	3	4	0	0	5	0	0	3	0	0	4	0	0	4	0	3

544

(b) OEI dataset JF	February-March atmospheric field																	
	THF SD highpass			500hPa omega SD highpass			850hPa v wind differences SD			Total Precip. differences SD			800hPa Eady Growth Rate			SLP		
	+	-	s	+	-	s	+	-	s	+	-	s	+	-	s	+	-	s
OI																		
GMPE																		
OSTIA																		
MEAN																		
Agreement score	0	0	0	2	0	0	2	0	0	4	0	0	0	0	0	5	0	0

545

546 **Table 3** Table showing where significant regression coefficients occur in regression maps of
 547 (a) the JF FDI and (b) the JF OEI, for indices derived from each dataset against atmospheric
 548 and storm-track variables. +, - and s denote positive, negative and symmetric regression cases
 549 respectively. Light blue indicates that the regression map shows regions of significance at
 550 $p < 0.2$, and dark blue indicates that there is significance at $p < 0.1$, after application of the False
 551 Discovery Rate. SD = monthly standard deviation of daily highpass-filtered or daily-
 552 differenced data.

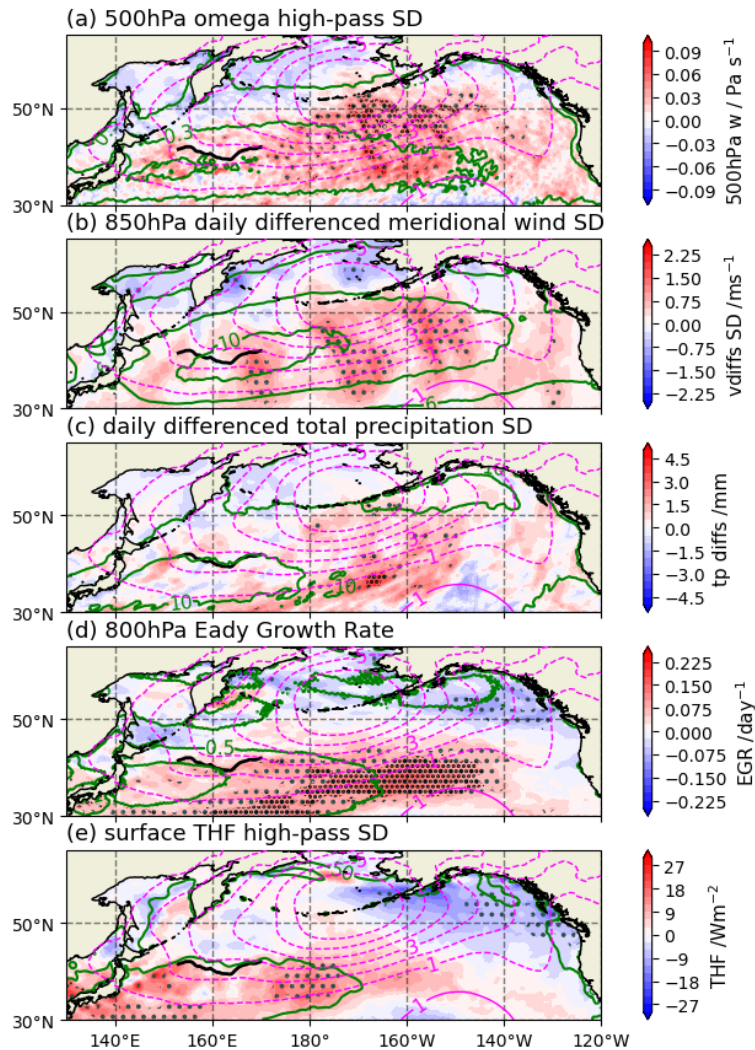
553

554 The FDI shows closer agreement than the OEI for the significant regressions of storm-track
 555 fields against different dataset indices. For example, all three datasets show significant positive

556 regressions of the meridional wind differences against the FDI. However, for the OEI there is
557 less agreement between the different dataset indices. A simple agreement score is employed to
558 quantify this. If two of the three dataset indices (the mean indices are not included) agree in
559 showing regions of significance, points are awarded, two for $p < 0.1$, one for $p < 0.2$. Based on
560 the agreement score, there is a moderate to high level of agreement between the FDI regressions
561 for the different dataset indices in positive regressions which suggests that these features are
562 robust. For the OEI, there are fewer instances of agreement in significance, and much of the
563 agreement is at a lower significance threshold. When considering SLP, indicative of impacts
564 on large-scale atmospheric variability, both the OEI and FDI show good agreement between
565 the different datasets for the positive phase regression, while disagreeing on the negative and
566 symmetric regressions.

567

568 Next we present the results from the OEI regressions using the mean OEI averaged over three
569 datasets (Figure 8). All significant regressions occur for the positive regression case, when the
570 OE is shifted northwards. A significant ($p < 0.1$) low sea-level pressure (SLP) monopole is
571 centred over the Aleutian Islands (dashed magenta contours in Figure 8), and significant
572 regression coefficients for the storm-track metrics occur consistently on the southern flank of
573 the low-pressure anomalies: a northward shift of the OE is associated one month later with
574 increases in the standard deviation of meridional wind and total precipitation daily differences,
575 and an increase in 800hPa EGR, mainly between $180\text{-}140^\circ\text{W}$ (Figure 8d). This indicates an
576 eastward extension of storm-track activity downstream of the OE, with the OE leading by one
577 month. The daily-differenced parameters are associated with the transit of low-pressure
578 systems along the storm-track. The increased variability reflects the increased passage of fronts
579 or stronger storms, which are accompanied by changes in wind direction; and the warm and
580 cold sectors, where rainfall and meridional winds are more vigorous and also more changeable.
581 Significant increases in omega at 500hPa are located on the northern flank of the climatological
582 storm-track (figure 8a). Descending cold air (positive omega) is associated with the cold sector
583 behind the cold front, and ascending warm air (negative omega) is linked to the warm front
584 ahead of the warm sector, which will combine to increase variability of omega when storm-
585 track activity increases.



586

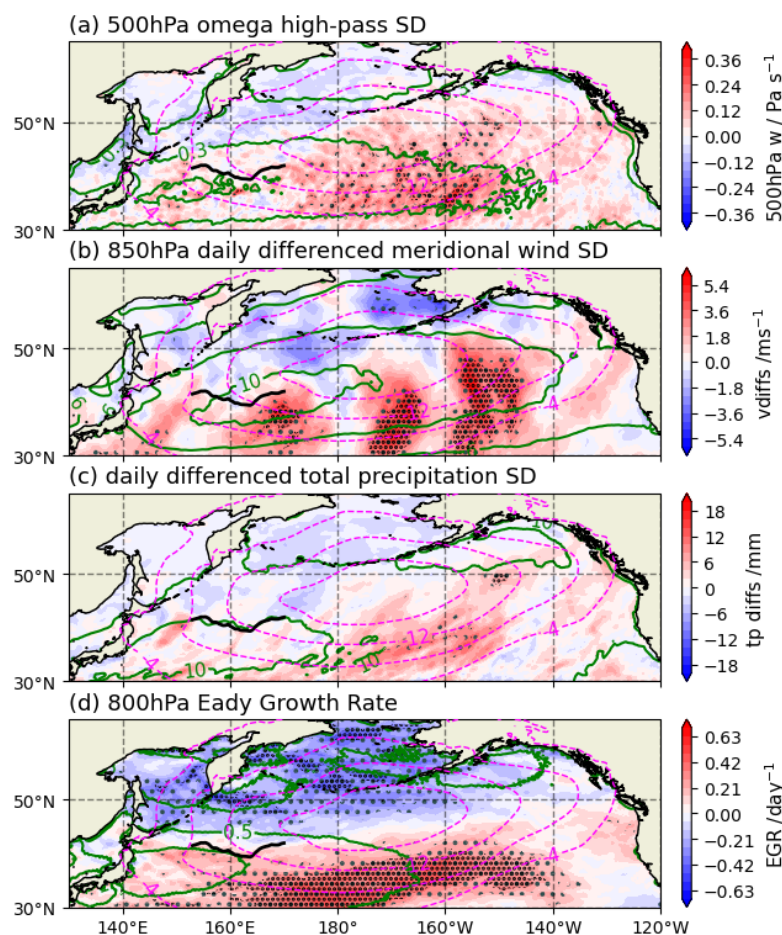
587 **Figure 8.** Asymmetric (positive) regression on the dataset averaged OEI, 153-173°E for JF,
 588 for various FM atmospheric fields related to storm tracks. Maps are only shown where there
 589 are significant regression coefficients ($p < 0.2$), after the FDR is applied. Shading shows
 590 significance at $p < 0.2$ (coarse gray) or $p < 0.1$ (fine black). The contours of the SLP regression
 591 coefficients are shown in magenta, dotted for negative values and the zero contour is omitted
 592 (contour interval 1hPa). The solid black line shows the mean position of the OE front. Green
 593 contours show the climatological mean values of the respective atmospheric field. Contour
 594 intervals: 0.1 Pa s^{-1} (highpass-filtered omega SD); 2 ms^{-1} (v wind differences); 5 mm (total
 595 precipitation differences); 0.25 day^{-1} (EGR); 50 W m^{-2} (highpass-filtered turbulent heat fluxes).
 596

597 There is a positive association of the highpass-filtered THF with the OEI in positive regression,
 598 such that as the OEI becomes more positive, the heat flux variability increases just downstream
 599 of the OE region ($180\text{-}160^\circ\text{W}, 40^\circ\text{N}$) and to the south of the OE front (Figure 8e). The heat flux
 600 variability reflects the passage of the warm and cold sectors of a low-pressure system over the
 601 ocean; fluxes are upwards (positive) in the cold sector and downwards (negative) in the warm
 602 sector. Increased variability reflects an increased frequency of large positive and negative

603 values, which indicates increased storm-track activity as the OEI becomes more positive and
604 the front shifts northwards.

605

606 The regressions using the FDI show similar asymmetry to those based on the OEI. Meridional
607 wind shows a higher level of significance, and significance is more widespread for EGR
608 (Figure 9b, Table 3). Significance for omega at 500hPa are shifted southwards relative to those
609 for the OEI (Figure 9a). An increase in SST front disturbance from climatology is associated
610 with a low-pressure monopole a month later, with increased storm-track activity to the south
611 of the monopole.



612

613 **Figure 9.** As for Figure 8, except for regression on the average FDI, 155-164°E for positive
614 regressions. SLP contours are 4hPa. Note the colorbar scales are different from those in Figure
615 8.

616

617 Significant negative regressions are found when precipitation differences and omega (Table
618 3a) are regressed onto the mean FDI, but not for any of the individual datasets. These are not
619 shown in Figure 9, but are located upstream over the Sea of Okhotsk. There is also higher

620 agreement in the THF regression field between datasets for the FDI compared with OEI (Table
621 3) although this is not reflected in the mean index.

622
623 A notable aspect of these results is that the spatial patterns of significant regression coefficients
624 for the OEI and FDI in positive regression are very similar (Figures 8a-d and Figure 9), as
625 discussed in section 4.3. Specifically, the positive phases of the FDI and OEI are significantly
626 positively correlated ($r=0.52-0.59$), which suggests that the atmospheric response to each time
627 series in this phase would show similarities. Both indices project onto a pressure monopole
628 near the Aleutians (thin magenta lines show SLP in Figures 8 and 9). For the OEI, this indicates
629 a deepening of the climatological low pressure centered over the Aleutians, enhancing the
630 storm-track activity to the south. For the FDI, the monopole is shifted about 10° further south,
631 representing a southward displacement of the climatological low pressure. However,
632 significant storm-track metric responses are at very similar locations, on the southern flank of
633 this monopole. This indicates a strengthening and eastward extension of the climatological
634 storm-track steered by the enhanced poleward low-pressure region, as seen by comparing with
635 the location of the climatological values of the metrics (green contours). However, the
636 associated SST front changes associated with the very similar atmospheric responses are
637 different: for the OEI, it is a northward (southward) shift that increases (decreases) storm track
638 activity when the OE is in the positive phase (recall that the mean is subtracted in asymmetric
639 regressions). For the FDI, it is increased (decreased) disturbance from the mean, when the FDI
640 is already in the positive (increased displacement) phase, that is associated with the increased
641 (decreased) storm track variability. As seen in section 4.4, the FDI is an indicator of ocean
642 mesoscale eddy variability, so an increase in mesoscale eddy activity polewards of 40°N in the
643 central OE region is associated with increased storm-track activity.

644
645 To summarise the regression patterns for the FDI, in positive regressions (when the central OE
646 has an SST front displaced from the mean), changes in frontal disturbance have a significant
647 association with atmospheric variability (Table 3, Figure 9), indicating a downstream extension
648 or contraction of the storm-track as the positive FDI decreases or increases.

649

650 **5. Discussion and Summary**

651 We have shown that the OEI and subsequent regressions with atmospheric fields are dataset
652 dependent. Dataset selection is therefore an important aspect of a study's design and we would
653 recommend considering more than one dataset, along with using different metrics for

654 quantifying the SST fronts, to identify the robust features of air-sea interactions. SSTs used in
655 ERA5 in particular appear to be an outlier, showing weaker correlations with indices from
656 other datasets, and markedly different responses in regression maps. On average, ERA5
657 underestimates the SST variability in the KE region compared with an ensemble median of
658 SST datasets (Yang et al., 2021). These WBC regions have higher mesoscale eddy activity,
659 and it is possible that the SSTs used in ERA5 underestimate the SST fluctuations in this region
660 (Sroka et al., 2022). Calculating the amplitude of the SST mesoscale eddy activity for ERA5,
661 as for Figure 7a, confirms this (not shown).

662

663 We have found that the storm-track related air-sea interactions associated with the OE have a
664 significant asymmetric component. The fact that the positive regression phase for OEI and FDI
665 show very similar regression patterns (even closer than some OEI regression patterns from
666 different datasets) is noteworthy, and the timeseries show moderate positive correlations in the
667 positive phase. Both the northward shift of the OE in its positive phase, and the increasing shift
668 away from climatology for the FDI, are associated with increased downstream storm-track
669 activity and a monopole of low pressure near the Aleutian Islands. Another striking feature of
670 the FDI is that although correlations between the indices of the different datasets are no better
671 than those of the OEI, there is much more agreement between the regressions of the FDI from
672 different datasets.

673

674 The FDI is a novel index designed to quantify the disruption of the maximum SST gradient in
675 the central section of the OE. Increased mesoscale eddy activity in the SST field to the north
676 acts against the mean poleward SST gradient and the local SST gradient maximum at around
677 40°N, resulting in a disrupted maximum SST gradient and an increased FDI. The increased
678 mesoscale eddy activity and increased FDI are associated with increased storm-track activity.
679 This is consistent with previous model results (Ma et al., 2017; Jia et al., 2020) where
680 atmospheric baroclinic growth is modified via the presence of oceanic eddies. This results in
681 increased moisture content in the marine atmospheric boundary layer, and enhanced
682 cyclogenesis via moist baroclinic instability. The origins of this eddy activity have not been
683 determined, and will be left for future research, however there may be links with KE variability
684 and the strength of the Isoguchi jets (Isoguchi et al., 2006; Seo et al., 2014; Sugimoto and
685 Hanawa, 2011; Sugimoto 2014).

686

687 The northward shift of the OE is easier to understand in the context of storm-tracks being
688 anchored on the northern flanks of SST fronts; high baroclinicity is maintained by the contrast
689 in heat supply across the SST front (e.g. Nakamura et al., 2008), so that shifts in the SST fronts
690 will have an impact on the storm track. Considering the central section of the OE, the
691 displacement of the SST front from climatology as measured by the FDI, has an impact on the
692 storm-track.

693

694 The association of the FDI with mesoscale eddy variability is interesting but cannot be easily
695 explained within the scope of this paper. Eddies can erode the SST front through increased
696 surface heat loss (e.g. Nonaka et al., 2009). However, recent studies indicate that eddies may
697 also act to maintain SST fronts, through vertical heat transport replenishing the heat lost from
698 the surface (Jing et al., 2021). Tang et al. (2022) report that most eddies weaken the SST
699 gradient within the eddies, but induce the redistribution of the SST front in the surrounding
700 ocean, which varies according to whether eddies are cyclonic or anticyclonic.

701

702 The OEI appears to perform poorly as a measure of high-frequency (i.e., storm-track related)
703 air-sea interaction based on using a one-month lag between the OEI and the subsequent storm-
704 track variable and when considering consistency between datasets. Previous research has
705 identified more significant air-sea-interactions than found here due to different research foci.
706 For example, Frankignoul et al. (2011) examine the OEI in the context of large-scale
707 atmospheric variability. Indeed, their results are consistent with those presented here as they
708 find little significance at one month lag but stronger signals at lags of two to five months. In
709 addition, our focus is winter, whereas Frankignoul et al. (2011) find a strong response based
710 on all months as well as with an August-October index and November-January atmospheric
711 fields. The growth in high-frequency weather systems as indicated by the storm-track response
712 may subsequently lead to changes in diabatic heating and momentum and heat fluxes by these
713 high-frequency systems, with subsequent changes in the jetstream. However, in the present
714 study we do not consider the FDI impacts at different lag times which may reveal such
715 responses. Neither do we compare early and late winter differences, or differences at other
716 times in the year. Investigating the physical mechanisms which link fluctuations in the positive
717 FDI to changes in the storm track is also left for future research. Here we simply present the
718 FDI as a complementary approach to identifying high-frequency air-sea interactions, which at
719 short timescales with a lag of around one month, produces more consistent air-sea interaction
720 results when using different datasets to derive the index than does the OEI.

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The key findings of the study are summarised below.

1. The OEIs obtained from different datasets show considerable variation. Correlations are stronger on seasonal or bimonthly timescale, but weak on a subseasonal scale. We do not recommend using indices such as the OEI for identifying subseasonal variability in air-sea interactions, due to the large discrepancies between datasets at this temporal scale. Identifying a single *best* dataset to use for defining the OEI is not clearly achievable. However we advise against the use of ERA5 SST data, as it is a clear outlier.
2. These differences arise from slight differences in the representation of SST gradients in the considered datasets, particularly in the more complex central regions where there are parallel fronts or fronts are weak.
3. When used to diagnose air-seas interactions, the OEIs from different SST products can produce different spatial patterns, which may have significant impacts on feature identification and explanations.
4. We develop a new index, the FDI, to quantify the complex central region of the OE, and the extent to which the SST gradient deviates from climatology. This new index is associated with the strength of the SST gradient at 40°N. This gradient is in turn affected by fluctuations in ocean mesoscale eddy activity to the north and south.
5. The FDI has an asymmetric association with air-sea interactions. When the average deviation from climatology is high, a further increase in disturbance is associated with an eastward extension of the storm track. These responses are linked to ocean mesoscale eddy activity in the region.
6. Similarly, the response of storm-track metrics to the north-south shifts of the OE front is asymmetric. It is the positive regression phase that is significant (when the OE front is shifted to the north).
7. The FDI produces a more robust air-sea interaction signal with storm-track metrics than the OEI, for the one-month time lag considered here, as there is more agreement between the regressions based on indices calculated from the different SST datasets and the significance of the regressions is often at a higher threshold. The agreement in the FDI regression results across datasets is notable as the correlations between the FDI from different datasets are actually similar to (or in the case of GMPE, lower than) the correlations between the different OEIs, yet more consistent regression results are obtained.

754 **8.** An important feature of the OEI and FDI regressions is that the positive regression phase
755 produces very similar spatial regression patterns. This reflects the fact that when the FDI
756 and OEI are partitioned by OEI phase, positive correlations are found in the positive
757 phase.

758

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766

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